

Various GLGM examples

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```
library('mapmisc')

## Loading required package: sp
## Loading required package: raster
## map images will be cached in /tmp/RtmpMsyjpT/mapmiscCache

library("geostatsp")

## Loading required package: Matrix

data('swissRain')

havePackages = c(
  'INLA' = requireNamespace('INLA', quietly=TRUE)
)

print(havePackages)

## INLA
## TRUE

swissRain$lograin = log(swissRain$rain)
swissAltitudeCrop = raster::mask(swissAltitude,swissBorder)
```

number of cells... smaller is faster but less interesting

```
fact

## [1] 1

(Ncell = 25*fact)

## [1] 25
```

standard formula

```

if(all(havePackages)) {

  swissFit = glgm(
    formula = lograin~ CHE_alt,
    data = swissRain,
    grid = Ncell,
    buffer = 10*1000,
    covariates=swissAltitudeCrop,
    family="gaussian",
    prior = list(
      sd=c(2, 0.05),
      sdObs = 1,
      range=c(500000, 0.5)),
    control.inla = list(strategy='gaussian')
  )
  knitr::kable(swissFit$parameters$summary, digits=3)

  swissExc = excProb(
    x=swissFit, random=TRUE,
    threshold=0)

  plot(swissExc, breaks = c(0, 0.2, 0.8, 0.95, 1.00001),
    col=c('green','yellow','orange','red'))

  plot(swissBorder, add=TRUE)

  swissExcP = excProb(
    swissFit$inla$marginals.predict, 3,
    template=swissFit$raster)
  plot(swissExcP, breaks = c(0, 0.2, 0.8, 0.95, 1.00001),
    col=c('green','yellow','orange','red'))
  plot(swissBorder, add=TRUE)

  matplot(
    swissFit$parameters$sd$posterior[, 'x'],
    swissFit$parameters$sd$posterior[, c('y', 'prior')],
    lty=1, col=c('black','red'), type='l',
    xlab='sd', ylab='dens', xlim = c(0,5))

  matplot(
    swissFit$parameters$range$posterior[, 'x'],
    swissFit$parameters$range$posterior[, c('y', 'prior')],

```

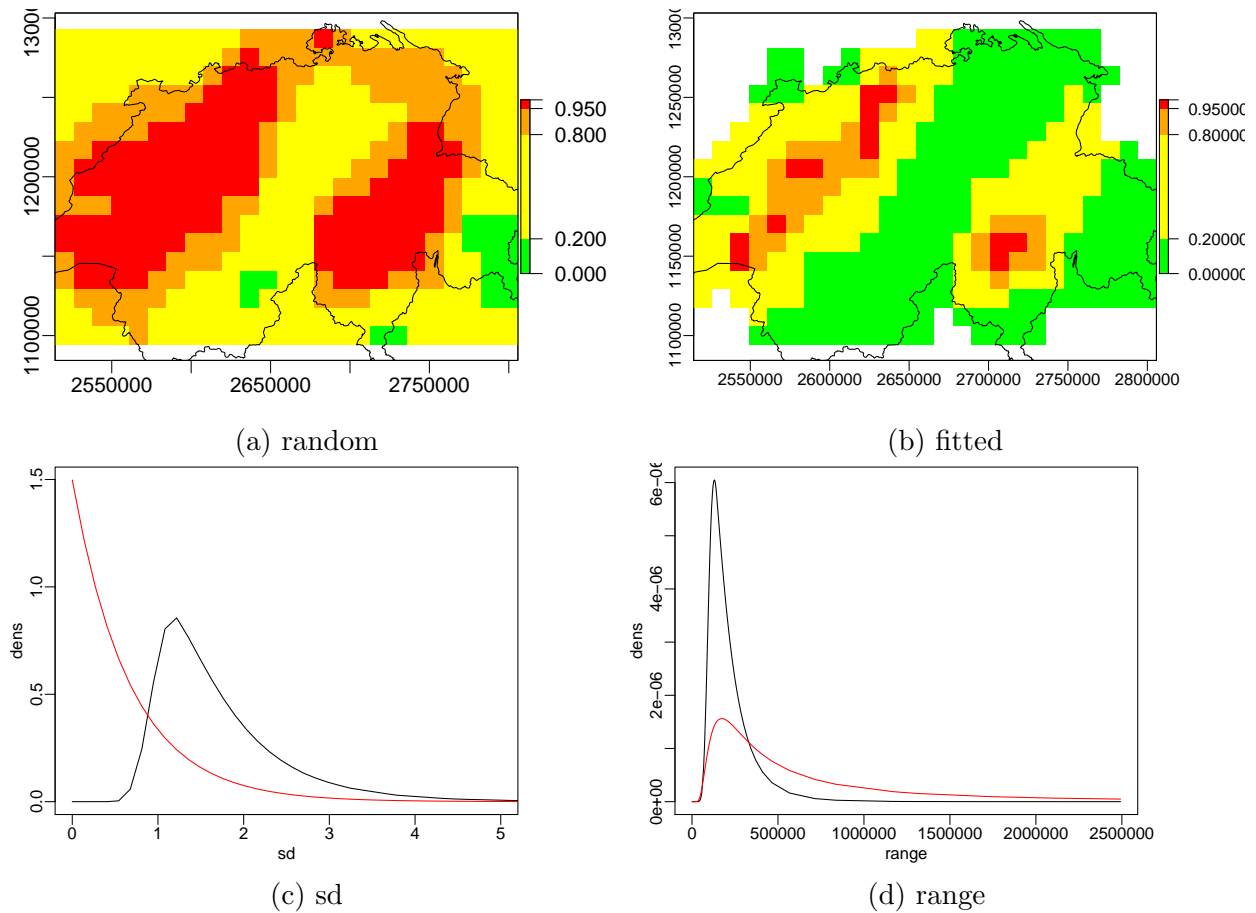


Figure 1: Swiss rain as in help file

```
lty=1, col=c('black','red'), type='l',
xlab='range', ylab='dens')
}
```

non-parametric elevation effect

```
altSeq = exp(seq(
  log(100), log(5000),
  by = log(2)/5))

swissAltCut = raster::cut(
  swissAltitudeCrop,
  breaks=altSeq
)
names(swissAltCut) = 'bqrnt'

if(all(havePackages)) {
```

```

swissFitNp = glgm(
  formula = lograin ~ f(bqrnt, model = 'rw2', scale.model=TRUE,
    values = 1:length(altSeq),
    prior = 'pc.prec', param = c(0.1, 0.01)),
  data=swissRain,
  grid = Ncell,
  covariates=swissAltCut,
  family="gaussian", buffer=20000,
  prior=list(
    sd=c(u = 0.5, alpha = 0.1),
    range=c(50000,500000),
    sdObs = c(u=1, alpha=0.4)),
  control.inla=list(strategy='gaussian')
)
knitr::kable(swissFitNp$parameters$summary, digits=3)

matplot(
  altSeq,
  exp(swissFitNp$inla$summary.random$bqrnt[,
    c('0.025quant', '0.975quant', '0.5quant')]),
  log='xy',
  xlab = 'elevation', ylab='rr',
  type='l',
  lty = 1,
  col=c('grey', 'grey', 'black')
)

swissExcP = excProb(swissFitNp$inla$marginals.predict,
  3, template=swissFitNp$raster)
plot(swissExcP, breaks = c(0, 0.2, 0.8, 0.95, 1.00001),
  col=c('green', 'yellow', 'orange', 'red'))
plot(swissBorder, add=TRUE)
}

```

intercept only, named response variable. legacy priors

```

if(all(havePackages)) {
  swissFit = glgm("lograin", swissRain, Ncell,
    covariates=swissAltitude, family="gaussian", buffer=20000,
    priorCI=list(sd=c(0.2, 2), range=c(50000,500000), sdObs = 2),
    control.inla=list(strategy='gaussian')
  )
}

```

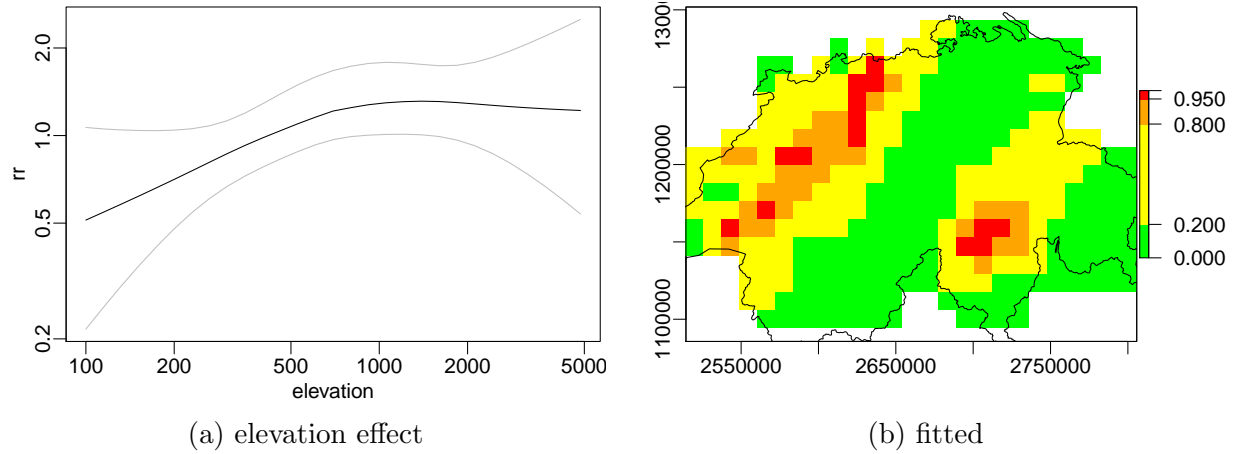


Figure 2: Swiss rain elevation rw2

```
knitr::kable(swissFit$parameters$summary[,c(1, 3:5, 8)], digits=4)
}
```

	mean	0.025quant	0.5quant	0.975quant	meanExp
(Intercept)	2.4836	1.7228	2.5127	3.0930	12.5582
CHE alt	-0.0001	-0.0004	-0.0001	0.0002	1.0034
range/1000	99.8303	47.7009	88.0418	218.7268	NA
sdNugget	0.3140	0.2083	0.3039	0.4962	NA
sd	0.9239	0.6282	0.8909	1.4407	NA

intercept only, add a covariate just to confuse glgm.

```
if(all(havePackages)) {

  swissFit = glgm(
    formula=lograin~1,
    data=swissRain,
    grid=Ncell,
    covariates=swissAltitude,
    family="gaussian", buffer=20000,
    priorCI=list(sd=c(0.2, 2), range=c(50000,500000)),
    control.inla=list(strategy= 'gaussian'),
    control.family=list(hyper=list(prec=list(prior="loggamma", param=c(.1, .1))))
  )

  knitr::kable(swissFit$parameters$summary[,c(1, 3:5, 8)], digits=3)

  swissExc = excProb(
    swissFit$inla$marginals.random$space, 0,
    template=swissFit$raster)
  plot(swissExc, breaks = c(0, 0.2, 0.8, 0.95, 1.00001),
```

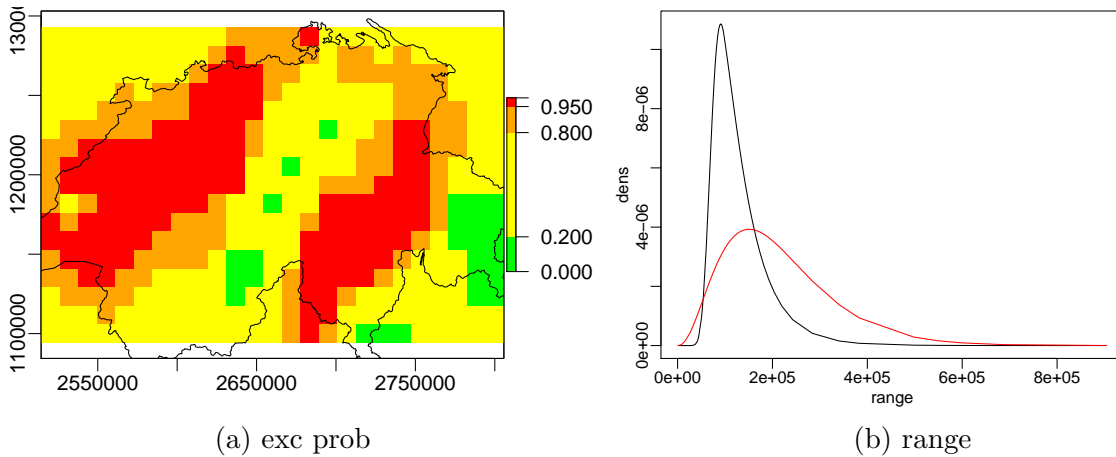


Figure 3: Swiss intercept only

```
col=c('green','yellow','orange','red'))
plot(swissBorder, add=TRUE)

matplot(
  swissFit$parameters$range$posterior[, 'x'],
  swissFit$parameters$range$posterior[, c('y', 'prior')],
  lty=1, col=c('black', 'red'), type='l',
  xlab='range', ylab='dens')
}
```

covariates are in data

```
newdat = swissRain
newdat$elev = extract(swissAltitude, swissRain)
if(all(havePackages)) {
  swissFit = glgm(lograin ~ elev + land,
    newdat, Ncell,
    covariates=list(land=swissLandType),
    family="gaussian", buffer=40000,
    priorCI=list(sd=c(0.2, 2), range=c(50000, 500000)),
    control.inla = list(strategy='gaussian'),
    control.family=list(hyper=list(prec=list(prior="loggamma",
      param=c(.1, .1))))
)
knitr::kable(swissFit$parameters$summary, digits=3)

plot(swissFit$raster[['predict.mean']])
plot(swissBorder, add=TRUE)
```

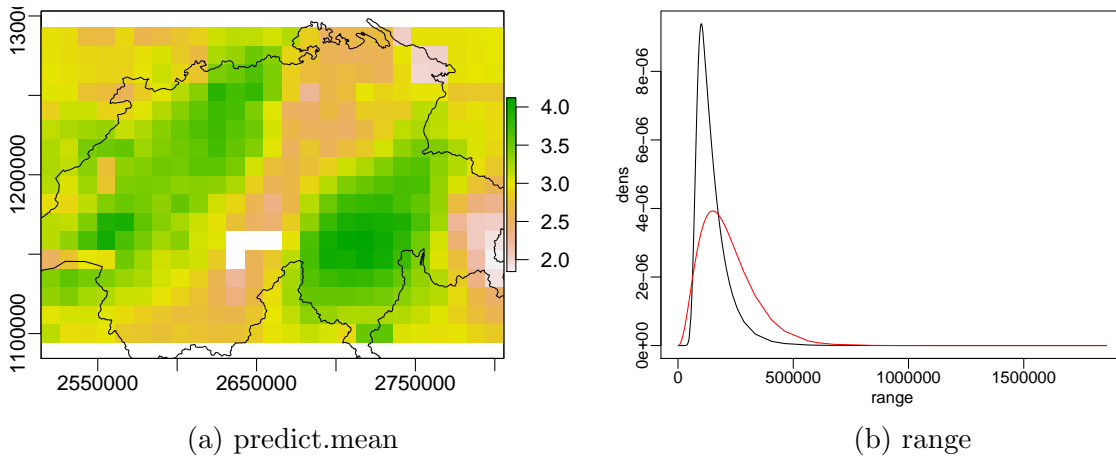


Figure 4: covaraites in data

```
matplot(
  swissFit$parameters$range$posterior[, 'x'],
  swissFit$parameters$range$posterior[, c('y', 'prior')],
  lty=1, col=c('black', 'red'), type='l',
  xlab='range', ylab='dens')
}
```

formula, named list elements

```
if(all(havePackages)) {

  swissFit = glgm(lograin~ elev,
    swissRain, Ncell,
    covariates=list(elev=swissAltitude),
    family="gaussian", buffer=20000,
    priorCI=list(sd=c(0.2, 2), range=c(50000,500000)),
    control.mode=list(theta=c(1.9,0.15,2.6),restart=TRUE),
    control.inla = list(strategy='gaussian'),
    control.family=list(hyper=list(prec=list(prior="loggamma",
      param=c(.1, .1))))
  )
  swissFit$parameters$summary[,c(1,3,5)]
}

##               mean      0.025quant    0.975quant
## (Intercept)  2.467153e+00  1.7089676475  3.083815e+00
## elev        -8.510456e-05 -0.0004023545  2.312653e-04
## range/1000   1.117355e+02  52.0062614630  2.537475e+02
## sdNugget     3.342323e-01  0.2323364213  4.985337e-01
```

```
## sd          9.646891e-01  0.6452409785 1.560966e+00
```

categorical covariates

```
if(all(havePackages)) {
  swissFit = glgm(
    formula = lograin ~ elev + factor(land),
    data = swissRain, grid = Ncell,
    covariates=list(elev=swissAltitude,land=swissLandType),
    family="gaussian", buffer=20000,
    prior=list(sd=c(0.2, 2), range=c(50000,500000)),
    control.inla=list(strategy='gaussian'),
    control.family=list(hyper=list(
      prec=list(prior="loggamma",
        param=c(.1, .1))))
  )

  knitr::kable(swissFit$parameters$summary[,c(1,3,5)], digits=3)

  plot(swissFit$raster[['predict.mean']])
  plot(swissBorder, add=TRUE)

  matplot(
    swissFit$parameters$range$posterior[, 'x'],
    swissFit$parameters$range$posterior[,c('y', 'prior')],
    lty=1, col=c('black', 'red'), type='l',
    xlab='range', ylab='dens')
}
```

put some missing values in covariates also dont put factor() in formula

```
temp = values(swissAltitude)
temp[seq(10000,12000)] = NA
values(swissAltitude) = temp
if(all(havePackages)) {

  swissFitMissing = glgm(rain ~ elev + land,swissRain, Ncell,
    covariates=list(elev=swissAltitude,land=swissLandType),
    family="gaussian", buffer=20000,
    priorCI=list(sd=c(0.2, 2), range=c(50000,500000)),
    control.inla = list(strategy='gaussian'),
    control.family=list(hyper=list(prec=list(prior="loggamma",
```

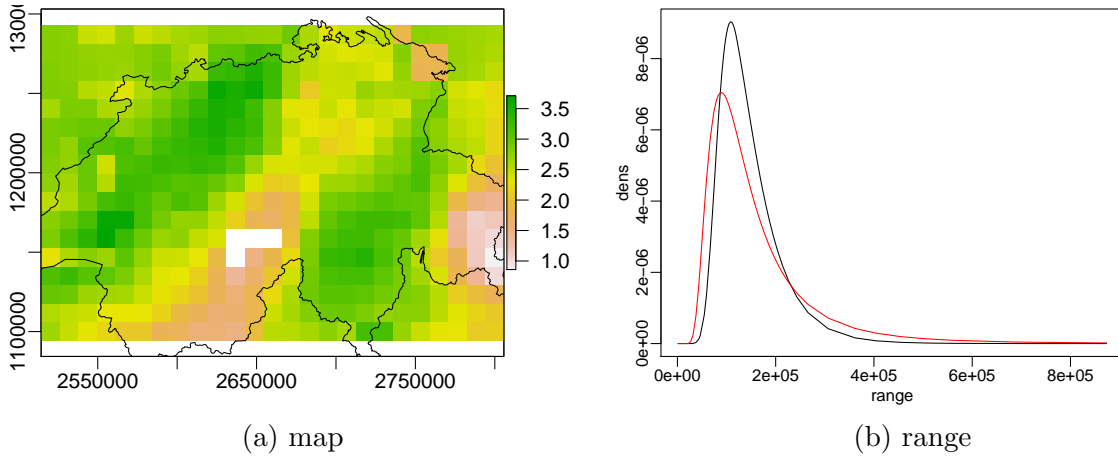



Figure 5: categorical covariates

```

    param=c(.1, .1)))
)
knitr::kable(swissFitMissing$parameters$summary[,1:5], digits=3)
}

```

	mean	sd	0.025quant	0.5quant	0.975quant
(Intercept)	27.005	3.288	20.522	27.009	33.458
elev	-0.004	0.003	-0.011	-0.004	0.002
landMixed forests	-4.328	3.262	-10.734	-4.332	2.097
landGrasslands	-3.145	4.922	-12.818	-3.150	6.544
landCroplands	-9.438	4.218	-17.724	-9.444	-1.133
landUrban and built-up	-8.045	5.490	-18.829	-8.052	2.764
landEvergreen needleleaf forest	-12.130	6.283	-24.469	-12.138	0.242
landWater bodies	-15.767	8.056	-31.576	-15.782	0.104
landDeciduous needleleaf forest	-8.997	8.021	-24.751	-9.006	6.795
landDeciduous broadleaf forest	8.229	8.015	-7.544	8.230	23.979
landOpen shrublands	-11.727	11.050	-33.414	-11.744	10.032
landPermanent Wetlands	-21.531	10.893	-42.873	-21.560	-0.051
range/1000	207.499	114.905	56.430	184.827	494.694
sdNugget	11.302	1.511	9.695	11.267	13.229
sd	0.574	0.150	0.216	0.489	1.627

covariates are in data, interactions

```

newdat = swissRain
newdat$elev = extract(swissAltitude, swissRain)
if(all(havePackages)) {
  swissFit = glm(

```

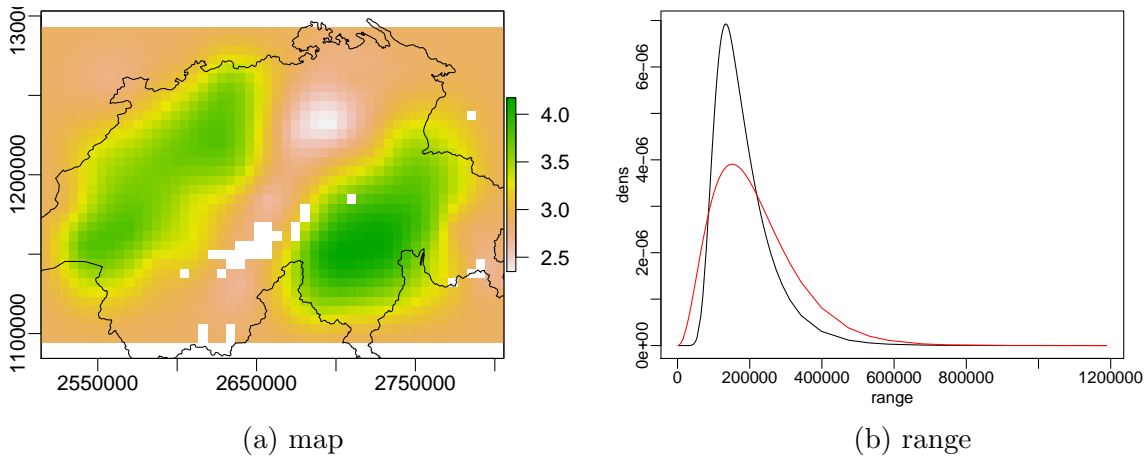


Figure 6: interactions

```

formula = lograin ~ elev : land,
data=newdat,
grid=squareRaster(swissRain,50),
covariates=list(land=swissLandType),
family="gaussian", buffer=0,
priorCI=list(sd=c(0.2, 2), range=c(50000,500000)),
control.inla = list(strategy='gaussian'),
control.family=list(hyper=list(prec=list(prior="loggamma",
param=c(.1, .1))))
)

knitr::kable(swissFit$parameters$summary, digits=3)

plot(swissFit$raster[['predict.mean']])
plot(swissBorder, add=TRUE)

matplot(
swissFit$parameters$range$posterior[, 'x'],
swissFit$parameters$range$posterior[, c('y', 'prior')],
lty=1, col=c('black', 'red'), type='l',
xlab='range', ylab='dens')
}

```

these tests are time consuming, so only run them if the **fact** variable is set to a value above 1.

```

data('loaloe')
rcl = rbind(
  # wetlands and mixed forests to forest

```

```

    c(5,2),c(11,2),
# savannas to woody savannas
    c(9,8),
    # croplands and urban changed to crop/natural mosaic
    c(12,14),c(13,14))
ltLoaR = reclassify(ltLoa, rcl)
levels(ltLoaR) = levels(ltLoa)

elevationLoa = elevationLoa - 750
elevLow = reclassify(elevationLoa, c(0, Inf, 0))
elevHigh = reclassify(elevationLoa, c(-Inf, 0, 0))

covList = list(elLow = elevLow, elHigh = elevHigh,
               land = ltLoaR, evi=eviLoa)

if(all(havePackages) & fact > 1) {

loaFit = glm(
  y ~ land + evi + elHigh + elLow +
  f(villageID, prior = 'pc.prec', param = c(log(2), 0.5),
    model="iid"),
  loaloa,
  Ncell,
  covariates=covList,
  family="binomial", Ntrials = loaloa$N,
  shape=2, buffer=25000,
  prior = list(
    sd=log(2),
    range = list(prior = 'invgamma', param = c(shape=2,rate=1))),
  control.inla = list(strategy='gaussian')
)

loaFit$par$summary[,c(1,3,5)]

plot(loaFit$raster[['predict.exp']])

matplot(
  loaFit$parameters$range$posterior[, 'x'],
  loaFit$parameters$range$posterior[,c('y', 'prior')],
  lty=1, col=c('black', 'red'), type='l',
  xlab='range', ylab='dens')

```

```
}
```

```
if(all(havePackages) & fact > 1 ) {  
  
  # prior for observation standard deviation  
  swissFit = glgm( formula="lograin",data=swissRain, grid=Ncell,  
    covariates=swissAltitude, family="gaussian", buffer=20000,  
    prior=list(sd=0.5, range=200000, sdObs=1),  
    control.inla = list(strategy='gaussian')  
  )  
}
```

a model with little data, posterior should be same as prior

```
data2 = SpatialPointsDataFrame(cbind(c(1,0), c(0,1)),  
  data=data.frame(y=c(0,0), offset=c(-50,-50), x=c(-1,1)))  
  
if(all(havePackages) & fact > 1) {  
  
  resNoData = res = glgm(  
    data=data2, grid=Ncell,  
    formula=y~1 + x+offset(offset),  
    prior = list(sd=0.5, range=0.1),  
    family="poisson",  
    buffer=0.5,  
    control.fixed=list(  
      mean.intercept=0, prec.intercept=1,  
      mean=0,prec=4),  
    control.mode = list(theta = c(0.651, 1.61), restart=TRUE),  
    control.inla = list(strategy='gaussian')  
  )  
  
  # beta  
  plot(res$inla$marginals.fixed[['x']], col='blue', type='l',  
    xlab='beta',lwd=3)  
  xseq = res$inla$marginals.fixed[['x']][,'x']  
  lines(xseq, dnorm(xseq, 0, 1/2),col='red',lty=2,lwd=3)  
  legend("topright", col=c("blue","red"),lty=1,legend=c("prior","post'r"))  
  
  # sd  
  matplot(  
    res$parameters$sd$posterior[, 'x'],
```

```

    res$parameters$sd$posterior[,c('y','prior')],
    xlim = c(0, 4),
    type='l', col=c('red','blue'),xlab='sd',lwd=3, ylab='dens')
  legend("topright", col=c("blue","red"),lty=1,legend=c("prior","post'r"))

# range
  matplot(
    res$parameters$range$posterior[, 'x'],
    res$parameters$range$posterior[,c('y','prior')],
    xlim = c(0, 1.5),
    type='l', col=c('red','blue'),xlab='range',lwd=3, ylab='dens')
  legend("topright", col=c("blue","red"),lty=1,legend=c("prior","post'r"))

    matplot(
    res$parameters$scale$posterior[, 'x'],
    res$parameters$scale$posterior[,c('y','prior')],
    xlim = c(0, 2/res$parameters$summary['range','0.025quant']),
    # ylim = c(0, 10^(-3)), xlim = c(0,1000),
    type='l', col=c('red','blue'),xlab='scale',lwd=3, ylab='dens')
  legend("topright", col=c("red","blue"),lty=1,legend=c("post'r","prior"))
}

```

```

if(all(havePackages) & fact > 1) {

  resQuantile = res = glgm(
    data=data2,
    grid=25,
    formula=y~1 + x+offset(offset),
    prior = list(
      sd=c(lower=0.2, upper=2),
      range=c(lower=0.02, upper=0.5)),
    family="poisson", buffer=1,
    control.fixed=list(
      mean.intercept=0, prec.intercept=1,
      mean=0,prec=4),
    control.inla = list(strategy='gaussian')
  )

# beta
  plot(res$inla$marginals.fixed[['x']], col='blue', type='l',

```

```

    xlab='beta',lwd=3)
xseq = res$inla$marginals.fixed[['x']][,'x']
lines(xseq, dnorm(xseq, 0, 1/2),col='red',lty=2,lwd=3)
legend("topright", col=c("blue","red"),lty=1,legend=c("prior","post'r"))

# sd
matplot(
  res$parameters$sd$posterior[, 'x'],
  res$parameters$sd$posterior[,c('y','prior')],
  xlim = c(0, 4),
  type='l', col=c('red','blue'),xlab='sd',lwd=3, ylab='dens')
legend("topright", col=c("blue","red"),lty=1,legend=c("prior","post'r"))

# range
matplot(
  res$parameters$range$posterior[, 'x'],
  res$parameters$range$posterior[,c('y','prior')],
  xlim = c(0, 1.2*res$parameters$summary['range','0.975quant']),
  # ylim = c(0, 1), ylim = c(0,5),
  type='l', col=c('red','blue'),xlab='range',lwd=3, ylab='dens')
legend("topright", col=c("red","blue"),lty=1,legend=c("post'r","prior"))

# scale
matplot(
  res$parameters$scale$posterior[, 'x'],
  res$parameters$scale$posterior[,c('y','prior')],
  xlim = c(0, 2/res$parameters$summary['range','0.025quant']),
  # ylim = c(0, 10^(-3)), ylim = c(0,1000),
  type='l', col=c('red','blue'),xlab='scale',lwd=3, ylab='dens')
legend("topright", col=c("red","blue"),lty=1,legend=c("post'r","prior"))
}

```

No data, legacy priors

```

if(all(havePackages) & fact > 1) {

resLegacy = res = glgm(data=data2,
  grid=20,
  formula=y~1 + x+offset(offset),
  priorCI = list(
    sd=c(lower=0.3,upper=0.5),
    range=c(lower=0.25, upper=0.4)),

```

```

family="poisson",
buffer=0.5,
control.fixed=list(
  mean.intercept=0,
  prec.intercept=1,
  mean=0, prec=4),
control.inla = list(strategy='gaussian'),
control.mode=list(theta=c(2, 2),restart=TRUE)
)

# intercept
plot(res$inla$marginals.fixed[['(Intercept)']], col='blue', type='l',
      xlab='intercept',lwd=3)
xseq = res$inla$marginals.fixed[['(Intercept)']][,'x']
lines(xseq, dnorm(xseq, 0, 1),col='red',lty=2,lwd=3)
legend("topright", col=c("blue","red"),lty=1,legend=c("prior","post'r"))

# beta
plot(res$inla$marginals.fixed[['x']], col='blue', type='l',
      xlab='beta',lwd=3)
xseq = res$inla$marginals.fixed[['x']][,'x']
lines(xseq, dnorm(xseq, 0, 1/2),col='red',lty=2,lwd=3)
legend("topright", col=c("blue","red"),lty=1,legend=c("prior","post'r"))

# sd
matplot(
  res$parameters$sd$posterior[, 'x'],
  res$parameters$sd$posterior[, c('y', 'prior')],
  type='l', col=c('red', 'blue'),xlab='sd',lwd=3, ylab='dens')
legend("topright", col=c("blue","red"),lty=1,legend=c("prior","post'r"))

# range
matplot(
  res$parameters$range$posterior[, 'x'],
  res$parameters$range$posterior[, c('y', 'prior')],
  type='l', col=c('red', 'blue'),xlab='range',lwd=3, ylab='dens')
legend("topright", col=c("blue","red"),lty=1,legend=c("prior","post'r"))
}

```

specifying spatial formula

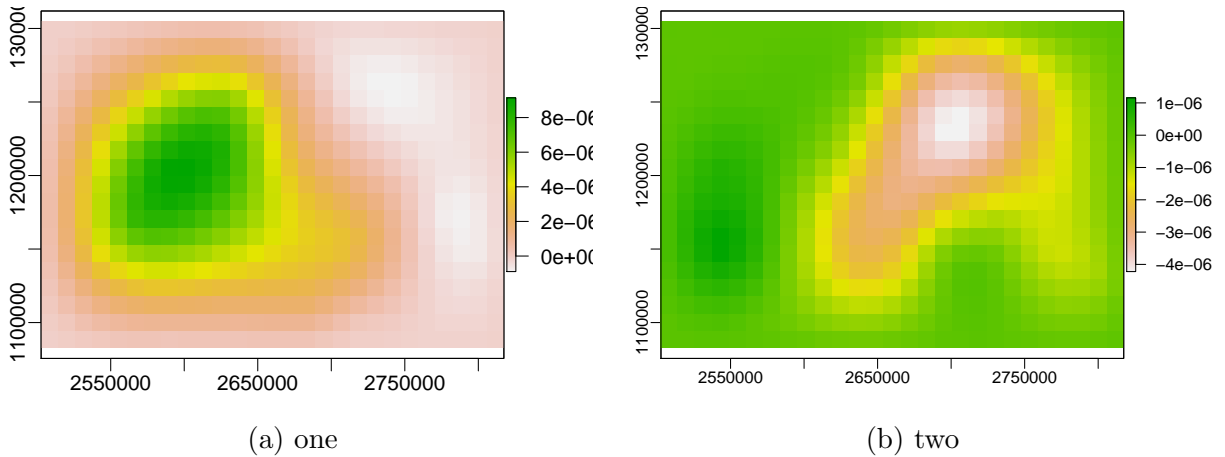


Figure 7: spatial formula provided

```

swissRain$group = 1+rbinom(length(swissRain), 1, 0.5)
theGrid = squareRaster(swissRain, Ncell, buffer=10*1000)

if(all(havePackages)) {
  swissFit = glm(
    formula = rain ~ 1,
    data=swissRain,
    grid=theGrid,
    family="gaussian",
    spaceFormula = ~ f(space, model='matern2d',
      nrow = nrow(theGrid), ncol = ncol(theGrid),
      nu = 1, replicate = group),
    control.inla = list(strategy='gaussian'),
  )

  if(!is.null(swissFit$inla$summary.random$space)) {
    swissFit$rasterTwo = setValues(
      raster::brick(swissFit$raster, nl=2),
      as.matrix(swissFit$inla$summary.random$space[
        ncell(theGrid)+values(swissFit$raster[['space']]),
        c('mean', '0.5quant')]))
    plot(swissFit$raster[['random.mean']])

    plot(swissFit$rasterTwo[['mean']])
  }
}

```