

Package ‘BsplineQuantReg’

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Type Package

Title 'Constrained Quantile Regression with B-Splines'

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Description Quantile regression with B-splines under shape constraints.
The initial version with cubic splines is now augmented with splines of degree 1 to 4. Constraints for degrees 3 (monotone) and 4 (monotone and convex) use the Karlin-Studden SOCP characterization for the sign of the polynomial, while other constraints applied at the knots are added as linear problems. The method for cubic splines is described in Abbes (2026) <[doi:10.5281/zenodo.17427913](https://doi.org/10.5281/zenodo.17427913)>. Other formulations are simple consequences of the other given references. This R implementation is intended for demonstration and prototyping. All B-spline and polynomial functions have been rewritten for consistency. An equivalent Python package is available at <<https://pypi.org/project/BsplineQuantRegpy/>>.

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URL <https://github.com/alexandreabbes/BsplineQuantReg>,
<https://doi.org/10.5281/zenodo.17427913>

BugReports <https://github.com/alexandreabbes/BsplineQuantReg/issues>

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apply_karlin_quadratic

Apply Karlin-Studden constraints for a quadratic polynomial

Description

For a quadratic polynomial $p(u) = a*u^2 + b*u + c$ on $[0,1]$, this function applies the Karlin-Studden SOCP constraints to ensure $p(u) \geq 0$ or $p(u) \leq 0$ on $[0,1]$.

Usage

apply_karlin_quadratic(p2, p1, p0, z0, sign = 1)

Arguments

p2	Coefficient of u^2
p1	Coefficient of u
p0	Constant term
z0	Auxiliary SOCP variable
sign	Sign of the constraint (+1 for ≥ 0 , -1 for ≤ 0)

Value

List of CVXR constraints

Bspline_base	<i>Build B-spline basis in piecewise polynomial form Computes local polynomial coefficients for each B-spline basis function on each interval. Polynomials are expressed in the canonical basis Uses De Boor's recursion formula.</i>
--------------	---

Description

Build B-spline basis in piecewise polynomial form Computes local polynomial coefficients for each B-spline basis function on each interval. Polynomials are expressed in the canonical basis Uses De Boor's recursion formula.

Usage

```
Bspline_base(sn, degree = 3, der = NULL, verbose = FALSE)
```

Arguments

sn	Extended knot vector (including endpoint repetitions) This means if $t_0..t_{kn}$ is the set of knot then sn should be given as a vector with "degree" times t_0 and t_{kn} at the beginning and the ends. its length is number of intervals+1+2*degree.
degree	B-spline degree (default = 3 for cubic)
der	Derivative order (0 = original basis)
verbose	boolean FALSE (default) or TRUE.

Value

A list containing:

base	Coefficients in the local bases, in the form of an 3-d array [j,nu,coeff], j : the number of the spline in the basis, nu: the number of the interval in the extended notation, coeff : the coefficients in decreasing order convention on the local bases $(t-s_{nu})^l$, $l=3..1$ base[j,,] is a matrix of piecewise polynomial function compatible with the pp-form.
------	---

base0	Coefficients in canonical basis (centered at 0) (1, t, t ² , t ³) centered at the interval origin.
ext_knot	Extended knot vector
knot	Effective knot partition including ends)
degree	Spline degree
n_splines	Number of basis functions
deriv_order	Applied derivative order

Examples

```
sn <- c(0,0,0,0,1,2,3,4,5,5,5,5)
basis <- Bspline_base(sn, degree=3)
x=(0:(5*100))/100
y=bs_direct(basis,x)
matplot(x,t(y))
#or simple:
#view_basis(basis)
```

Bspline_deriv	<i>Differentiate a B-spline basis</i>
---------------	---------------------------------------

Description

Computes the basis of order der derivatives of a B-spline basis.

Usage

```
Bspline_deriv(bspline, der = 2, verbose = FALSE)
```

Arguments

bspline	Object returned by Bspline_base
der	Derivative order
verbose	boolean FALSE (default) or TRUE.

Value

A list similar to Bspline_base for the derivative basis

bspline_to_deriv_coeffs_cubic

*normalized first and second derivative coefficients on each interval.
for a cubic B-spline basis*

Description

normalized first and second derivative coefficients on each interval. for a cubic B-spline basis

Usage

```
bspline_to_deriv_coeffs_cubic(tn, degree = 3, x_values = 0, verbose = FALSE)
```

Arguments

tn	Knot vector (effective partition, not extended)
degree	Spline degree (default = 3)
x_values	Evaluation points for design matrix (0 = no evaluation)
verbose	boolean FALSE (default) or TRUE.

Value

A list containing:

d0	Design matrix (if x_values provided)
d1	First derivative coefficients [a3, a2, a1] for each interval
d2	Second derivative values at knot

bspline_to_deriv_coeffs_lin

Derivative coefficients for linear B-spline to

Description

Computes normalized first derivative coefficients for linear B-splines. For linear splines, the derivative is constant on each interval.

Usage

```
bspline_to_deriv_coeffs_lin(tn, degree = 1, x_values = 0, verbose = FALSE)
```

Arguments

tn	Knot vector (effective partition)
degree	Spline degree (should be 1)
x_values	Evaluation points for design matrix (0 = no evaluation)
verbose	logical; if TRUE, print progress messages

Value

A list containing:

d0	Design matrix (if x_values provided)
d1	First derivative values (constant per interval)

bspline_to_deriv_coeffs_quad
quadratic B-spline derivative coefficients

Description

Computes normalized first and second derivative coefficients for quadratic B-splines on each interval.

Usage

```
bspline_to_deriv_coeffs_quad(tn, degree = 2, x_values = 0, verbose = FALSE)
```

Arguments

tn	Knot vector (effective partition)
degree	Spline degree (should be 2)
x_values	Evaluation points for design matrix (0 = no evaluation)
verbose	logical; if TRUE, print progress messages

Value

A list containing:

d0	Design matrix (if x_values provided)
d1	First derivative coefficients [a1, a0] for each interval
d2	Second derivative values (constant per interval)

bspline_to_deriv_coeffs_quart

Convert quartic B-spline to derivative coefficients

Description

Computes normalized first, second, and third derivative coefficients for quartic B-splines on each interval.

Usage

```
bspline_to_deriv_coeffs_quart(knot, degree = 4, x_values = 0)
```

Arguments

knot	Knot vector (effective partition)
degree	Spline degree (should be 4)
x_values	Evaluation points for design matrix

Value

A list containing:

d0	Design matrix (if x_values provided)
d1	First derivative coefficients [a3, a2, a1, a0] for each interval
d2	Second derivative coefficients [a2, a1, a0] for each interval
d3	Third derivative values at knot (linear constraints)

bs_direct

Direct evaluation of a B-spline basis

Description

Computes the values of all B-spline basis functions at given points.

Usage

```
bs_direct(Basis, x_values)
```

Arguments

Basis	Object returned by Bspline_base
x_values	Vector of evaluation points

Value

Matrix of basis function values (n_splines x length(x_values))

change_polynomial_base_taylor	<i>Change polynomial basis (Taylor expansion)</i>
-------------------------------	---

Description

Converts a polynomial expressed in the basis $(t-a)^k$ to its representation in the basis $(t-b)^k$ using Taylor's formula. $P(t) = \sum c_k (t-a)^k$ $P(t) = \sum c''_k (t-b)^k$

Usage

```
change_polynomial_base_taylor(coeffs_a, a, b)
```

Arguments

coeffs_a	Coefficients in basis centered at a (decreasing powers)
a	Original expansion point
b	New expansion point

Value

Coefficients in basis centered at b

make_spline	<i>Create a callable spline object</i>
-------------	--

Description

Transforms a spline regression result into a callable function that can be evaluated at any point, while preserving access to parameters.

Usage

```
make_spline(result)
```

Arguments

result	A list returned by quantile_spline or one of the degree-specific functions
--------	--

Value

A function that can be called as `result(x)` and has attributes for `'degree'`, `'knot'`, `'coefficients'`, and `'status'`

polyadd

*Polynomial addition***Description**

Adds two polynomials represented by coefficients in decreasing power order.

Usage

```
polyadd(p1, p2, verbose = FALSE)
```

Arguments

p1	First polynomial (coefficient vector)
p2	Second polynomial (coefficient vector)
verbose	boolean FALSE (default) or TRUE.

Value

Coefficient vector of the sum

Examples

```
polyadd(c(1, 1), c(1, -1)) # returns c(2, 0)
```

polyderiv

*Polynomial derivative Computes the derivative of order der of a polynomial.***Description**

Polynomial derivative Computes the derivative of order der of a polynomial.

Usage

```
polyderiv(p, der = 1)
```

Arguments

p	Coefficient vector (decreasing powers)
der	Derivative order (default = 1)

Value

Coefficients of the derivative polynomial

Examples

```
# P(x) = x^2 -> P'(x) = 2x
polyderiv(c(1, 0, 0), 1) # returns c(2, 0)
```

polymul	<i>Polynomial multiplication</i>
---------	----------------------------------

Description

Multiplies two polynomials represented by coefficients in decreasing power order.

Usage

```
polymul(p1, p2, ord = 0, verbose = FALSE)
```

Arguments

p1	First polynomial (coefficient vector, decreasing powers)
p2	Second polynomial (coefficient vector, decreasing powers)
ord	Unused (compatibility parameter)
verbose	boolean FALSE (default) or TRUE.

Value

Coefficient vector of the product polynomial (decreasing powers)

Examples

```
# (1 + x) * (1 + x) = 1 + 2x + x^2
polymul(c(1, 1), c(1, 1)) # returns c(1, 2, 1)
```

poly_eval	<i>Evaluate polynomial</i>
-----------	----------------------------

Description

Evaluates a polynomial at one or more points.

Usage

```
poly_eval(p, xvalues)
```

Arguments

p	Coefficient vector (decreasing powers)
xvalues	vector at which to evaluate the polynomial

Value

Vector of same length as xvalues : polynomial values at the points xvalues

Examples

```
# P(x) = 1 + x + x^2
poly_eval(c(1, 1, 1), c(0, 1, 2)) # returns c(1, 3, 7)
```

```
print.callable_spline Print method for callable spline
```

Description

Print method for callable spline

Usage

```
## S3 method for class 'callable_spline'
print(x, ...)
```

Arguments

x	A callable spline object
...	Additional arguments

```
print.quantile_spline Print method for quantile_spline results
```

Description

Print method for quantile_spline results

Usage

```
## S3 method for class 'quantile_spline'
print(x, ...)
```

Arguments

x	Result object from quantile_spline
...	Additional arguments

Description

This function provides a unified interface for quantile regression with B-splines of degrees 1 to 4, with shape constraints (monotonicity, convexity, third derivative).

Usage

```
quantile_spline(
  xtab,
  ytab,
  knot,
  tau,
  degree = 3,
  monot = 0,
  convcons = 0,
  der3cons = 0,
  solver = "CLARABEL",
  weight = NULL,
  verbose = FALSE,
  callable = FALSE
)
```

Arguments

xtab	Predictor vector (x)
ytab	Response vector (y)
knot	Knot vector or number of knots (quantiles are then used)
tau	Quantile (between 0 and 1)
degree	Spline degree: 1 (linear), 2 (quadratic), 3 (cubic), or 4 (quartic)
monot	Monotonicity constraint vector per interval: 1 = increasing, -1 = decreasing, 0 = unconstrained. If scalar, repeated.
convcons	Convexity constraint vector: For degree 1: not available (ignored) For degree 2: per interval (1 = convex, -1 = concave) For degree 3: per knot (1 = convex, -1 = concave) For degree 4: per interval (1 = convex, -1 = concave)
der3cons	Third derivative constraint: For degree 1: not available (third derivative = 0) For degree 2: not available (third derivative = 0) For degree 3: per interval (1 = positive, -1 = negative) For degree 4: per knot (1 = positive, -1 = negative)
solver	CVXR solver to use (default = "CLARABEL")
weight	Observation weights (default = 1 for all)
verbose	logical; if TRUE, print progress messages
callable	render the final container object callable: y=Bspline(x) or y=Bspline(x,Bvalues) for evaluation at x

Value

A list containing coefficients, degree, and knots

References

- Abbes, A. (2025). *Quantile regression with cubic polynomial splines under shape constraints with applications*. Zenodo. doi:10.5281/zenodo.16999784
- Karlin, S., & Studden, W. J. (1966). *Tchebycheff Systems: With Applications in Analysis and Statistics*. Interscience.

See Also

[SplineLinearQuant](#), [SplineQuadraticQuant](#), [SplineCubicQuant](#), [SplineQuarticQuant](#)

Examples

```
# Generate data
set.seed(42)
x <- seq(0, 1, length.out = 100)
y <- 2*x + sin(6*pi*x)/2 + rnorm(100, 0, 0.05)
knot <- quantile(x, probs = seq(0, 1, length.out = 10))

# Linear spline (degree 1) with increasing constraint
fit_lin <- quantile_spline(x, y, knot, tau = 0.5, degree = 1, monot = 1)

# Quadratic spline (degree 2) with convexity constraint
fit_quad <- quantile_spline(x, y, knot, tau = 0.5, degree = 2, convcons = 1)

# Cubic spline (degree 3) with both constraints
fit_cubic <- quantile_spline(x, y, knot, tau = 0.5, degree = 3,
                           monot = 1, convcons = 1)

# Quartic spline (degree 4) with all constraints
fit_quart <- quantile_spline(x, y, knot, tau = 0.5, degree = 4,
                           monot = 1, convcons = 1, der3cons = 1)
```

reduce_pol

Reduce polynomial

Description

Removes leading zeros from a polynomial coefficient vector.

Usage

```
reduce_pol(p, verbose = FALSE)
```

Arguments

p	Polynomial coefficient vector(coef in decreasing order)
verbose	boolean FALSE (default) or TRUE.

Value

Reduced vector (without leading zeros)

Examples

```
reduce_pol(c(0,0, 1, 1))
```

SplineConstQuantRegBs1

Wrapper function for linear spline quantile regression

Description

This is a convenience wrapper for SplineLinearQuant.

Usage

```
SplineConstQuantRegBs1(
  xtab,
  ytab,
  knot,
  tau,
  monot = 0,
  solver = "OSQP",
  weight = NULL,
  verbose = FALSE
)
```

Arguments

xtab	Predictor vector (x)
ytab	Response vector (y)
knot	Knot vector or number of knots
tau	Quantile (between 0 and 1)
monot	Monotonicity constraint vector per interval: 1 = increasing, -1 = decreasing, 0 = unconstrained
solver	CVXR solver to use (default = "OSQP")
weight	Observation weights (default = 1 for all)
verbose	logical; if TRUE, print progress messages

Value

Same as SplineLinearQuant

SplineConstQuantRegBs2	<i>Wrapper function for quadratic spline quantile regression Previous version notation style This is a convenience wrapper for SplineQuadraticQuant.</i>
------------------------	--

Description

Wrapper function for quadratic spline quantile regression Previous version notation style This is a convenience wrapper for SplineQuadraticQuant.

Usage

```
SplineConstQuantRegBs2(  
  xtab,  
  ytab,  
  knot,  
  tau,  
  monot = 0,  
  convcons = 0,  
  solver = "OSQP",  
  weight = NULL,  
  verbose = FALSE  
)
```

Arguments

xtab	Predictor vector (x)
ytab	Response vector (y)
knot	Knot vector or number of knots
tau	Quantile (between 0 and 1)
monot	Monotonicity constraint vector per interval: 1 = increasing, -1 = decreasing, 0 = unconstrained
convcons	Convexity constraint vector per interval: 1 = convex, -1 = concave, 0 = unconstrained
solver	CVXR solver to use (default = "OSQP")
weight	Observation weights (default = 1 for all)
verbose	logical; if TRUE, print progress messages

Value

Same as SplineQuadraticQuant

SplineConstQuantRegBs3

Wrapper function for Cubic spline quantile regression

Description

This is a convenience wrapper for SplineCubicQuant with convention of previous versions SplineConstQuantRegBs3.

Usage

```
SplineConstQuantRegBs3(
  xtab,
  ytab,
  knot,
  tau,
  monot = 0,
  convcons = 0,
  der3cons = 0,
  solver = "CLARABEL",
  weight = NULL,
  verbose = FALSE
)
```

Arguments

xtab	Predictor vector (x)
ytab	Response vector (y)
knot	Knot vector or number of knot (quantiles are then used)
tau	Quantile (between 0 and 1)
monot	Monotonicity constraint vector per interval: 1 = increasing, -1 = decreasing, 0 = unconstrained. If scalar, repeated.
convcons	Convexity constraint vector per knot: 1 = convex, -1 = concave, 0 = unconstrained. If scalar, repeated.
der3cons	Constraint on the 3rd derivative (on esach intervall: -1: négative, 0: no constraint, 1: positive constraint)
solver	CVXR solver to use (default = "CLARABEL")
weight	Observation weights (default = 1 for all)
verbose	boolean FALSE (default) or TRUE.

Value

Same as SplineCubicQuant

SplineConstQuantRegBs4

Wrapper function for quartic spline quantile regression

Description

This is a convenience wrapper for SplineQuarticQuant that follows the same naming convention as SplineConstQuantRegBs3.

Usage

```
SplineConstQuantRegBs4(
  xtab,
  ytab,
  knot,
  tau,
  monot = 0,
  convcons = 0,
  der3cons = 0,
  solver = "CLARABEL",
  weight = NULL,
  verbose = FALSE
)
```

Arguments

xtab	Predictor vector (x)
ytab	Response vector (y)
knot	Knot vector or number of knot
tau	Quantile (between 0 and 1)
monot	Monotonicity constraint vector per interval: 1 = increasing, -1 = decreasing, 0 = unconstrained
convcons	Convexity constraint vector per interval: 1 = convex, -1 = concave, 0 = unconstrained
der3cons	Third derivative constraint vector at knot: 1 = positive third derivative, -1 = negative, 0 = unconstrained
solver	CVXR solver to use (default = "OSQP")
weight	Observation weights (default = 1 for all)
verbose	Logical; if TRUE, print progress messages

Value

Same as SplineQuarticQuant

SplineCubicQuant

*Constrained quantile regression with cubic splines***Description**

Performs quantile regression using cubic B-splines, with optional monotonicity constraints (via Karlin-Studden) and convexity constraints.

Usage

```
SplineCubicQuant(
  xtab,
  ytab,
  knot,
  tau,
  monot = 0,
  convcons = 0,
  der3cons = 0,
  solver = "CLARABEL",
  weight = NULL,
  verbose = FALSE
)
```

Arguments

xtab	Predictor vector (x)
ytab	Response vector (y)
knot	Knot vector or number of knot (quantiles are then used)
tau	Quantile (between 0 and 1)
monot	Monotonicity constraint vector per interval: 1 = increasing, -1 = decreasing, 0 = unconstrained. If scalar, repeated.
convcons	Convexity constraint vector per knot: 1 = convex, -1 = concave, 0 = unconstrained. If scalar, repeated.
der3cons	Constraint on the 3rd derivative (on each interval: -1: négative, 0: no constraint, 1: positive constraint)
solver	CVXR solver to use (default = "CLARABEL")
weight	Observation weights (default = 1 for all)
verbose	boolean FALSE (default) or TRUE.

Value

A list containing:

coefficients B-spline coefficients (including y mean)

degree	Spline degree (always 3)
ext_knot	ext_knot vector used
int_knot	knot vector

References

- Abbes, A. (2025). *Quantile regression with cubic polynomial splines under shape constraints with applications*. Zenodo. doi:10.5281/zenodo.16999784
- de Boor, C. (1978). *A Practical Guide to Splines*. Springer-Verlag. doi:10.1007/97814612-63333
- Karlin, S., & Studden, W. J. (1966). *Tchebycheff Systems: With Applications in Analysis and Statistics*. Interscience.
- Koenker, R., & Bassett, G. (1978). Regression Quantiles. *Econometrica*, 46(1), 33-50. doi:10.2307/1913643
- Koenker, R. (2025). quantreg: Quantile Regression. R package version 5.99. <https://CRAN.R-project.org/package=quantreg>
- Ng, P., & Maechler, M. (2024). cobs: Constrained B-Splines. R package version 1.3-8. <https://CRAN.R-project.org/package=cobs>

See Also

Related R packages:

- quantreg - Quantile regression with linear programming
- cobs - Constrained B-sines (linear and quadratic only)

Other implementations:

- MATLAB/Python versions: <https://github.com/alexandreabbes/Constrained-Quantile-Regression-with-c>

Examples

```
#optional set.seed(42)
x <- seq(0, 1, length=100)
y <- 2*x + sin(6*pi*x)/2 + rnorm(100, 0, 0.05)
knot <- quantile(x, probs=seq(0,1,length.out=10))

# Median quantile regression without constraints
fit <- SplineConstQuantRegBs3(x, y, knot, tau=0.5)

# With increasing monotonicity constraint
fit_monot <- SplineConstQuantRegBs3(x, y, knot, tau=0.5, monot=1)

# With convexity constraint
fit_convex <- SplineConstQuantRegBs3(x, y, knot, tau=0.5, convcons=1)
```

SplineLinearQuant	<i>Quantile regression with linear splines and monotonicity constraints</i>
-------------------	---

Description

Performs quantile regression using linear B-splines with monotonicity constraints. For linear splines, the derivative is constant on each interval, so monotonicity is a simple linear constraint on the derivative.

Usage

```
SplineLinearQuant(
  xtab,
  ytab,
  knot,
  tau,
  monot = 0,
  solver = "OSQP",
  weight = NULL,
  verbose = FALSE
)
```

Arguments

xtab	Predictor vector (x)
ytab	Response vector (y)
knot	Knot vector or number of knots
tau	Quantile (between 0 and 1)
monot	Monotonicity constraint vector per interval: 1 = increasing, -1 = decreasing, 0 = unconstrained
solver	CVXR solver to use (default = "OSQP")
weight	Observation weights (default = 1 for all)
verbose	logical; if TRUE, print progress messages

Value

A list containing coefficients, degree, and knots

SplineQuadraticQuant *Quantile regression with quadratic splines and shape constraints*

Description

Performs quantile regression using quadratic B-splines with: - Monotonicity: Karlin-Studden constraints on the derivative (linear) - Convexity: Karlin-Studden constraints on the second derivative (constant)

Usage

```
SplineQuadraticQuant(
  xtab,
  ytab,
  knot,
  tau,
  monot = 0,
  convcons = 0,
  solver = "OSQP",
  weight = NULL,
  verbose = FALSE
)
```

Arguments

xtab	Predictor vector (x)
ytab	Response vector (y)
knot	Knot vector or number of knots
tau	Quantile (between 0 and 1)
monot	Monotonicity constraint vector per interval: 1 = increasing, -1 = decreasing, 0 = unconstrained
convcons	Convexity constraint vector per interval: 1 = convex, -1 = concave, 0 = unconstrained
solver	CVXR solver to use (default = "OSQP")
weight	Observation weights (default = 1 for all)
verbose	logical; if TRUE, print progress messages

Value

A list containing coefficients, degree, and knots

SplineQuarticQuant	<i>Quantile regression with quartic splines and shape constraints</i>
--------------------	---

Description

Performs quantile regression using quartic (degree 4) B-splines with monotonicity (Karlin-Studden constraints on the cubic derivative), convexity (Karlin-Studden constraints on the quadratic second derivative), and third derivative constraints (linear at knot).

Usage

```
SplineQuarticQuant(
  xtab,
  ytab,
  knot,
  tau,
  monot = 0,
  convcons = 0,
  der3cons = 0,
  solver = "OSQP",
  weight = NULL,
  verbose = FALSE
)
```

Arguments

xtab	Predictor vector (x)
ytab	Response vector (y)
knot	Knot vector or number of knot
tau	Quantile (between 0 and 1)
monot	Monotonicity constraint vector per interval: 1 = increasing, -1 = decreasing, 0 = unconstrained
convcons	Convexity constraint vector per interval: 1 = convex, -1 = concave, 0 = unconstrained
der3cons	Third derivative constraint vector at knot: 1 = positive third derivative, -1 = negative, 0 = unconstrained
solver	CVXR solver to use (default = "OSQP")
weight	Observation weights (default = 1 for all)
verbose	Logical; if TRUE, print progress messages

Value

A list containing coefficients, degree, and knot

Spline_der_knot	<i>Derivatives at knot of a B-spline</i>
-----------------	--

Description

Computes derivative values of a B-spline at knot (efficient because it directly uses polynomial coefficients).

Usage

```
Spline_der_knot(Bsbase, der = 1)
```

Arguments

Bsbase	Object returned by Bspline_base
der	Derivative order (default = 1)

Value

Matrix of derivative values (n_splines x n_knot)

spline_eval	<i>Evaluate a B-spline</i>
-------------	----------------------------

Description

Evaluates a spline (linear combination of B-splines) at given points.

Usage

```
spline_eval(Bspline, x_values = NULL, Bvalues = NULL)
```

Arguments

Bspline	Spline object (list with coefficients on the Bspline basis, degree, extended knot)
x_values	Vector of evaluation points. By default, evaluation is calculated at the knots
Bvalues	: the values of the Bspline basis evaluated at the values x this increases the speed by avoiding re-doing the same calculations of the basis for each spline with the same knots.

Value

vector of same length as x_values, with Spline values at the requested points

Examples

```
{ # Create and evaluate a spline
# This function is also used when a Bspline object is rendered callable as a function
# with make_spline()
tn<-c(0,1,2,3,4,5)
x_values<-seq(0,5,length=100)
Bspline=list(degree=3, knot=tn,coefficients=runif(length(tn)+3-1))
y <- spline_eval(Bspline, x_values)
#alternatively compute the base before to optimize if needed
sn <- c(0,0,0,0,1,2,3,4,5,5,5,5)
Bsbase <- Bspline_base(sn, degree=3)
Bvalues <-bs_direct(Bsbase,x_values)
y <- spline_eval(Bspline=Bspline,x_values=x_values, Bvalues=Bvalues )}
```

test_karlin_simple	<i>Comprehensive test function</i>
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Description

Runs quantile regression tests with and without constraints, and displays results. Demo function.

Usage

```
test_karlin_simple(verbose = FALSE, degree = 3, seed = NULL)
```

Arguments

verbose	boolean FALSE (default) or TRUE.
degree	1, 2, 3 or 4 (default 3). The degree of the regression spline.
seed	(default=NULL) value for the random generator.

Value

No return value, produces plots.

Examples

```
test_karlin_simple()
```

view_basis	<i>Visualize a B-spline functions basis</i>
------------	---

Description

Plots all functions of a B-spline basis.

Usage

```
view_basis(BB, x_values = 0)
```

Arguments

BB	Object returned by Bspline_base
x_values	Vector of evaluation points for plotting (by default 100 points are computed in the knot range)

Value

No return value, called for side effects (generates a plot)

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