

Package ‘blocklength’

May 12, 2021

Type Package

Title Select an Optimal Block-Length to Bootstrap Dependent Data
(Block Bootstrap)

Version 0.1.4

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Description A set of functions to select the optimal block-length for a dependent bootstrap (block-bootstrap). Includes the Hall, Horowitz, and Jing (1995) <[doi:10.1093/biomet/82.3.561](https://doi.org/10.1093/biomet/82.3.561)> cross-validation method and the Politis and White (2004) <[doi:10.1081/ETC-120028836](https://doi.org/10.1081/ETC-120028836)> Spectral Density Plug-in method, including the Patton, Politis, and White (2009) <[doi:10.1080/07474930802459016](https://doi.org/10.1080/07474930802459016)> correction with a corresponding set of S3 plot methods.

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Encoding UTF-8

RoxygenNote 7.1.1

Suggests testthat, covr, parallel, knitr, rmarkdown

Imports tseries, stats

URL <https://alecstashevsky.com/r/blocklength>,
<https://github.com/Alec-Stashevsky/blocklength>

BugReports <https://github.com/Alec-Stashevsky/blocklength/issues>

VignetteBuilder knitr

NeedsCompilation no

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Repository CRAN

Date/Publication 2021-05-12 12:12:24 UTC

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hhj	<i>Hall, Horowitz, and Jing (1995) "HHJ" Algorithm to Select the Optimal Block-Length</i>
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Description

Perform the Hall, Horowitz, and Jing (1995) "HHJ" cross-validation algorithm to select the optimal block-length for a bootstrap on dependent data (block-bootstrap). Dependent data such as stationary time series are suitable for usage with the HHJ algorithm.

Usage

```
hhj(
  series,
  nb = 100L,
  n_iter = 10L,
  pilot_block_length = NULL,
  sub_sample = NULL,
  k = "two-sided",
  bofb = 1L,
  search_grid = NULL,
  grid_step = c(1L, 1L),
  cl = NULL,
  verbose = TRUE,
  plots = TRUE
)
```

Arguments

series	a numeric vector or time series giving the original data for which to find the optimal block-length for.
nb	an integer value, number of bootstrapped series to compute.
n_iter	an integer value, maximum number of iterations for the HHJ algorithm to compute.
pilot_block_length	a numeric value, the block-length (l^* in <i>HHJ</i>) for which to perform initial block bootstraps.
sub_sample	a numeric value, the length of each overlapping subsample, m in <i>HHJ</i> .

k	a character string, either "bias/variance", "one-sided", or "two-sided" depending on the desired object of estimation. If the desired bootstrap statistic is bias or variance then select "bias/variance" which sets $k = 3$ per HHJ. If the object of estimation is the one-sided or two-sided distribution function, then set $k = \text{"one-sided"}$ or $k = \text{"two-sided"}$ which sets $k = 4$ and $k = 5$, respectively. For the purpose of generating symmetric confidence intervals around an unknown parameter, $k = \text{"two-sided"}$ (the default) should be used.
bofb	a numeric value, length of the basic blocks in the <i>block-of-blocks</i> bootstrap, <i>see</i> <code>m =</code> for <code>tsbootstrap</code> and Kunsch (1989).
search_grid	a numeric value, the range of solutions around l^* to evaluate within the <i>MSE</i> function <i>after</i> the first iteration. The first iteration will search through all the possible block-lengths unless specified in <code>grid_step =</code> .
grid_step	a numeric value or vector of at most length 2, the number of steps to increment over the subsample block-lengths when evaluating the <i>MSE</i> function. If <code>grid_step = 1</code> then each block-length will be evaluated in the <i>MSE</i> function. If <code>grid_step > 1</code> , the <i>MSE</i> function will search over the sequence of block-lengths from 1 to <code>m</code> by <code>grid_step</code> . If <code>grid_step</code> is a vector of length 2, the first iteration will step by the first element of <code>grid_step</code> and subsequent iterations will step by the second element.
cl	a cluster object, created by package parallel , doParallel , or snow . If NULL, no parallelization will be used.
verbose	a logical value, if set to FALSE then no interim messages are output to the console. Error messages will still be output. Default is TRUE.
plots	a logical value, if set to FALSE then no interim plots are output to the console. Default is TRUE.

Details

The HHJ algorithm is computationally intensive as it relies on a cross-validation process using a type of subsampling to estimate the mean squared error (*MSE*) incurred by the bootstrap at various block-lengths.

Under-the-hood, `hhj()` makes use of `tsbootstrap`, *see* Trapletti and Hornik (2020), to perform the moving block-bootstrap (or the *block-of-blocks* bootstrap by setting `bofb > 1`) according to Kunsch (1989).

Value

an object of class 'hhj'

References

Adrian Trapletti and Kurt Hornik (2020). *tseries: Time Series Analysis and Computational Finance*. R package version 0.10-48.

Kunsch, H. (1989) The Jackknife and the Bootstrap for General Stationary Observations. *The Annals of Statistics*, 17(3), 1217-1241. Retrieved February 16, 2021, from <http://www.jstor.org/stable/2241719>

Peter Hall, Joel L. Horowitz, Bing-Yi Jing, On blocking rules for the bootstrap with dependent data, *Biometrika*, Volume 82, Issue 3, September 1995, Pages 561-574, DOI: doi: [10.1093/biomet/82.3.561#](https://doi.org/10.1093/biomet/82.3.561)

Examples

```
# Generate AR(1) time series
sim <- stats::arima.sim(list(order = c(1, 0, 0), ar = 0.5),
                        n = 500, innov = rnorm(500))

# Calculate optimal block length for series
hhj(sim, sub_sample = 10)

# Use parallel computing
library(parallel)

# Make cluster object with 2 cores
cl <- makeCluster(2)

# Calculate optimal block length for series
hhj(sim, cl = cl)
```

plot.hhj

Plot MSE Function for HHJ Algorithm

Description

S3 Method for objects of class 'hhj'

Usage

```
## S3 method for class 'hhj'
plot(x, iter = NULL, ...)
```

Arguments

x	an object of class 'hhj'
iter	a vector of hhj() iterations to plot. NULL. All iterations are plotted by default.
...	Arguments passed on to base::plot
	y the y coordinates of points in the plot, <i>optional</i> if x is an appropriate structure.

Value

No return value, called for side effects

Examples

```
# Generate AR(1) time series
sim <- stats::arima.sim(list(order = c(1, 0, 0), ar = 0.5),
                        n = 500, innov = rnorm(500))

# Generate 'hhj' class object of optimal block length for series
hhj <- hhj(sim, sub_sample = 10)

## S3 method for class 'hhj'
plot(hhj)
```

plot.pwsd

Plot Correlogram for Politis and White Auto–Correlation Implied Hypothesis Test

Description

S3 Method for objects of class 'pwsd' See ?plot.acf of the **stats** package for more customization options on the correlogram, from which plot.pwsd is based

Usage

```
## S3 method for class 'pwsd'
plot(x, c = NULL, main = NULL, ylim = NULL, ...)
```

Arguments

x	an object of class 'pwsd' or 'acf'
c	a numeric value, the constant which acts as the significance level for the implied hypothesis test. Defaults to $qnorm(0.975)$ for a two-tailed 95% confidence level. Politis and White (2004) suggest $c = 2$.
main	an overall title for the plot, if no string is supplied a default title will be populated. See title
ylim	a numeric of length 2 giving the y-axis limits for the plot
...	Arguments passed on to base::plot

y the y coordinates of points in the plot, *optional* if x is an appropriate structure.

Value

No return value, called for side effects

Examples

```
# Use S3 Method

# Generate AR(1) time series
sim <- stats::arima.sim(list(order = c(1, 0, 0), ar = 0.5),
                        n = 500, innov = rnorm(500))

b <- pwsd(sim, round = TRUE, correlogram = FALSE)
plot(b)
```

pwsd	<i>Politis and White (2004) Spectral Density "PWSA" Automatic Block-Length Selection</i>
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Description

Run the Automatic Block-Length selection method proposed by Politis and White (2004) and corrected in Patton, Politis, and White (2009). The method is based on spectral density estimation via flat-top lag windows of Politis and Romano (1995). This code was adapted from [b.star](#) to add functionality and include correlogram support including an S3 method, *see* Hayfield and Racine (2008).

Usage

```
pwsd(
  data,
  K_N = NULL,
  M_max = NULL,
  m_hat = NULL,
  b_max = NULL,
  c = NULL,
  round = FALSE,
  correlogram = TRUE
)
```

Arguments

data	an $n \times k$ data.frame, matrix, or vector (if $k = 1$) where the optimal block-length will be computed for each of the k columns.
K_N	an integer value, the maximum lags for the auto-correlation, ρ_k , which to apply the <i>implied hypothesis</i> test. Defaults to $\max(5, \log(N))$. <i>See</i> Politis and White (2004) footnote c.
M_max	an integer value, the upper-bound for the optimal number of lags, M , to compute the auto-covariance for. <i>See</i> Theorem 3.3 (ii) of Politis and White (2004).

m_hat	an integer value, if set to NULL (the default), then m_hat is estimated as the smallest integer after which the correlogram appears negligible for K_N lags. In problematic cases, setting m_hat to an integer value can be used to override the estimation procedure.
b_max	a numeric value, the upper-bound for the optimal block-length. Defaults to <code>ceiling(min(3 * sqrt(n), n / 3))</code> per Politis and White (2004).
c	a numeric value, the constant which acts as the significance level for the implied hypothesis test. Defaults to <code>qnorm(0.975)</code> for a two-tailed 95% confidence level. Politis and White (2004) suggest <code>c = 2</code> .
round	a logical value, if set to FALSE then the final block-length output will not be rounded, the default. If set to TRUE the final estimates for the optimal block-length will be rounded to whole numbers.
correlogram	a logical value, if set to TRUE a plot of the correlogram (<i>i.e.</i> a plot of $R(k)$ vs. k) will be output to the console. If set to FALSE, no interim plots will be output to the console, but may be plotted later using the corresponding S3 method, plot.pwsd .

Value

an object of class 'pwsd'

References

Andrew Patton, Dimitris N. Politis & Halbert White (2009) Correction to "Automatic Block-Length Selection for the Dependent Bootstrap" by D. Politis and H. White, *Econometric Review*, 28:4, 372-375, DOI: doi: [10.1080/07474930802459016](https://doi.org/10.1080/07474930802459016)

Dimitris N. Politis & Halbert White (2004) Automatic Block-Length Selection for the Dependent Bootstrap, *Econometric Reviews*, 23:1, 53-70, DOI: doi: [10.1081/ETC120028836](https://doi.org/10.1081/ETC120028836)

Politis, D.N. and Romano, J.P. (1995), Bias-Corrected Nonparametric Spectral Estimation. *Journal of Time Series Analysis*, 16: 67-103, DOI: doi: [10.1111/j.14679892.1995.tb00223.x](https://doi.org/10.1111/j.14679892.1995.tb00223.x)

Tristen Hayfield and Jeffrey S. Racine (2008). Nonparametric Econometrics: The np Package. *Journal of Statistical Software* 27(5). DOI: doi: [10.18637/jss.v027.i05](https://doi.org/10.18637/jss.v027.i05)

Examples

```
# Generate AR(1) time series
sim <- stats::arima.sim(list(order = c(1, 0, 0), ar = 0.5),
                        n = 500, innov = rnorm(500))

# Calculate optimal block length for series
pwsd(sim, round = TRUE)

# Use S3 Method
b <- pwsd(sim, round = TRUE, correlogram = FALSE)
plot(b)
```

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