

Package ‘catnet’

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Title Categorical Bayesian Network Inference

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Description Structure learning and parameter estimation of discrete Bayesian networks using likelihood-based criteria. Exhaustive search for fixed node orders and stochastic search of optimal orders via simulated annealing algorithm are implemented.

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Imports methods, stats, utils, graphics

Suggests

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catnet.probs.R catnet.joint.prob.R catnet.marginal.prob.R
catnet.samples.R catnet.loglik.R catnet.entropy.R
catnet.categor.R catnet.dist.R catnet.plot.R catnet.find.R
catnet.search.R catnet.predict.R catnet.chisq.R catnet.histo.R
catnet.cluster.R catnet.bif.R catnet.quant.R catnet.pathway.R
zzz.R

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Description

catnet package provides tools for learning categorical Bayesian networks from data with focus on model selection. A Bayesian network is defined by a graphical structure in form of directed acyclic graph and a probability model given as a set of conditional distributions, one for each node in the network. Considered in the package are only categorical Bayesian networks - networks which nodes represent discrete random variables. The learning functions implemented in catnet are based on exhaustive search and output sets of networks with increasing complexity that fit the data according to MLE-based criteria. The final network selection is left to the user. These selected networks represent the relations between the node-variables in the data optimally.

Before starting to use the package, we suggest the user to take a look at some of the main objects used in catnet such as `catNetwork` and `catNetworkEvaluate` and then familiarize with the main search functions `cnSearchOrder` and `cnSearchSA`. More details and examples can be found in the manual pages and the vignettes accompanying the package.

Since catnet does not have its own plotting abilities, the user needs to setup some external tools in order to visualize networks, or more precisely, `catNetwork` objects. catnet provides interface to the Graphviz library for visualizing graphs. Graphviz is not a R-package but a platform independent library that the user have to install in advance on its machine in order to use this option.

In order to use Graphviz, in addition to installing the library, the user has to register a environmental variable with name `R_DOTVIEWER` with the path to the `Dot` executable file of Graphviz. The `Dot` routine generates a postscript or pdf-file from a text dot-file. Also, the user needs a postscript and pdf-viewer. The full path to it has to be given in another variable with name `R_PDFVIEWER`. Note that `R_PDFVIEWER` variable might be already setup. To check this call `Sys.getenv("R_PDFVIEWER")` in R.

The variables `R_DOTVIEWER` and eventually `R_PDFVIEWER` can be registered in the `.First` function residing in the `.Rprofile` initializing file.

Below we give two examples. On UNIX platform the user may use code like this one

```
.First <- function() {
.....
Sys.setenv(R_DOTVIEWER="/usr/bin/dot")
}
```

On Windows platform the user may have the following two lines in its `.First` function

```
.First <- function() {
.....
Sys.setenv(R_PDFVIEWER="\"C:/Program Files (x86)/Adobe/Reader 9.0/Reader/AcroRd32\"")
Sys.setenv(R_DOTVIEWER="\"C:/Program Files (x86)/Graphviz 2.26.3/bin/Dot\"")
}
```

Note that all paths in Windows should be embraced by comment marks, "\"".

Author(s)

N. Balov

alarm

The ALARM network

Description

ALARM stands for 'A Logical Alarm Reduction Mechanism' and it is a medical diagnostic alarm message system for patients monitoring developed by Beinlich et. al, (Beinlich, I., Suermondth, G., Chavez, R., Cooper, G., The ALARM monitoring system, 1989, In Proc. 2-nd Euro. Conf. on AI and Medicine). It is categorical Bayesian network has 37 nodes and 46 directed edges.

Usage

data(alarmnet)

Format

A data frame with 37 variables and 2000 samples.

Source

<http://www.norsys.com/netlib/alarm.htm>

breast

Breast cancer data

Description

Subclass Mapping: Identifying Common Subtypes in Independent Disease Data Sets

Usage

data(breast)

Format

A matrix containing 100 observations on 1214 genes.

Source

"<http://www.broadinstitute.org/cgi-bin/cancer/datasets.cgi>"

catNetwork-class	Class "catNetwork"
------------------	--------------------

Description

This is the base class in the `catnet` package for representing Bayesian networks with categorical values. It stores both the graph and probability structure of categorical Bayesian networks. Technically, `catNetwork` is a S4 type of R-class implemented in object-oriented style, with slots representing object components and members for accessing and manipulating class objects. Below we list the slots of `catNetwork` and some of its main members along with the functions for creating `catNetwork` objects.

Details

The `catNetwork` class provides a comprehensive general structure for representing discrete Bayesian networks by describing both the graph and probability structures. Although available for direct access, the class components, its slots, should not be manipulated directly but using the class members instead. A `catNetwork` object integrity can always be checked by calling `is(object, "catNetwork")`.

Objects from the Class

Objects can be created by calls of

```
cnNew(nodes, cats, parents, probs)
cnRandomCatnet(numnodes, maxParents, numCategories)
cnCatnetFromEdges(nodes, edges, numCategories)
cnCatnetFromSif(file)
```

Slots

`objectName` an optional object name of class character.

`numnodes`: an integer, the number of nodes in the object.

`nodes`: a vector specifying the node names.

`parents`: a list specifying the node parents. The list `parents` must be the same length as `nodes`. Parents are kept as indices in the `nodes` vector.

`categories`: a list of characters specifying a set of categorical values for each node.

`probabilities`: a numerical list that for each node specifies a discrete probability distribution - the distribution of the node conditional on its parent set. The elements of `probabilities` are lists themselves. See `cnProb` function for more details.

`maxParents`: an integer, the maximum number of node parents.

`maxCategories`: an integer, the maximum number of node categories.

`meta`: an object of class character storing some meta-data information.

`nodeComplexity`: a numerical vector, the node complexities.

nodeLikelihood: a numerical vector, the node likelihoods of the sample being used for estimation.

complexity: an integer, the network complexity

likelihood: a numerical, the total likelihood of the sample being used for estimation

nodeSampleSizes: a numerical vector, if the object is an estimate, the node sample sizes.

Methods

cnNew signature(nodes="vector", cats="list", parents="list", probs="list"): Creating a new class object.

cnRandomCatnet signature(numnodes="integer", maxParents="integer", numCategories="integer"): Creating a random class object.

cnCatnetFromEdges signature(nodes="vector", edges="list", numCategories="integer"): Deriving a class object from a list of edges.

cnCatnetFromSif signature(file="character"): Creating a class object from a file.

cnNumNodes signature(object="catNetwork"):

cnNodes signature(object="catNetwork", which="vector"):...

cnSubNetwork signature(object="catNetwork", nodeIndices="vector", indirectEdges="logical"):...

cnReorderNodes signature(object="catNetwork", nodeIndices="vector"):...

cnParents signature(object="catNetwork", which="vector"):...

cnMatParents signature(object="catNetwork", nodeorder="vector"):...

cnEdges signature(object="catNetwork", which="vector"):...

cnMatEdges signature(object="catNetwork"):...

cnProb signature(object="catNetwork"):...

cnSetProb signature(object="catNetwork", psamples="matrix"):...

cnPlot signature(object="catNetwork"):...

cnDot signature(object="catNetwork", file="character"):...

cnSamples signature(object="catNetwork", nsamples="integer"):...

cnSamplesPert signature(object="catNetwork", nsamples="integer", perturbations="matrix"):...

cnOrder signature(object="catNetwork"):...

cnLoglik signature(object="catNetwork", psamples="matrix"):...

cnComplexity signature(object="catNetwork"):...

cnEvaluate signature(object="catNetwork", psamples="matrix", perturbations="matrix", maxComplexity="integer"):...

cnPredict signature(object="catNetwork", psamples="matrix"):...

cnCompare signature(object1="catNetwork", object2="catNetwork"):...

Author(s)

N. Balov

See Also

[cnRandomCatnet](#), [cnCatnetFromEdges](#), [cnNew](#), [cnNodes](#), [cnEdges](#), [cnComplexity](#), [cnPlot](#)

Examples

```
set.seed(123)
cnet <- cnRandomCatnet(numnodes=10, maxParents=2, numCategories=2)
cnet
```

catNetworkDistance-class

Class "catNetworkDistance"

Description

This class contains a list of catNetworks and it is the output format of cnEvaluate function

Details

See in the manual of cnCompare function for description of different distance criteria.

Slots

hamm: an integer, the hamming distance between the parent matrices of the found networks and the original network.

hammexp: an integer, the hamming distance between the exponents of the parent matrices.

tp: an integer, the number of true positives directed edges.

fp: an integer, the number of false positives directed edges.

fn: an integer, the number of false negatives directed edges.

sp: a numeric, the specificity.

sn: a numeric, the sensitivity.

fscore: a numeric, the F-score.

skel.tp: an integer, the number of true positives undirected edges.

skel.fp: an integer, the number of false positives undirected edges.

skel.fn: an integer, the number of false negatives undirected edges.

order.fp: an integer, the number of false positive order relations.

order.fn: an integer, the number of false negative order relations.

markov.fp: an integer, the number of false positive Markov pairs.

markov.fn: an integer, the number of false negative Markov pairs.

KLdist: a numerical, the KL distance, currently inactive.

Methods

cnPlot signature(object="catNetworkDistance"): Draw some distance plots.

Author(s)

N. Balov

See Also

[catNetwork-class](#), [catNetworkEvaluate-class](#), [cnCompare](#), [cnPlot](#)

catNetworkEvaluate-class

Class "catNetworkEvaluate"

Description

This class contains a list of catNetworks together with some diagnostic metrics and information. catNetworkEvaluate objects are created automatically as result of calling cnEvaluate or one of the cnSearch functions.

Details

The class catNetworkEvaluate is used to output the result of two functions: cnEvaluate and cnSearchSA. The usage of it in the first case is explained next. The complexity and log-likelihood of the networks listed in nets slots are stored in complexity and loglik slots. Function cnEvaluate and cnCompare fills all the slots from hamm to markov.fn by comparing these networks with a given network. See in the manual of cnCompare function for description of different distance criteria. By calling cnPlot upon a catNetworkEvaluate object, some relevant comparison information can be plotted.

When catNetworkEvaluate is created by calling cnSearchSA or cnSearchSAcluster functions, complexity and loglik contains the information not about the networks in the nets list, but about the optimal networks found during the stochastic search process. Also, the slots from hamm to markov.fn are not used.

Slots

numnodes: an integer, the number of nodes in the network.

numsamples: an integer, the sample size used for evaluation.

nets: a list of resultant networks.

complexity an integer vector, the network complexity.

loglik a numerical vector, the likelihood of the sample being evaluated.

hamm: an integer vector, the hamming distance between the parent matrices of the found networks and the original network.

hammexp: an integer vector, the hamming distance between the exponents of the parent matrices.

tp: an integer vector, the number of true positives directed edges.
 fp: an integer vector, the number of false positives directed edges.
 fn: an integer vector, the number of false negatives directed edges.
 sp: a numeric vector, the specificity.
 sn: a numeric vector, the sensitivity.
 fscore: a numeric vector, the F-score.
 skel.tp: an integer vector, the number of true positives undirected edges.
 skel.fp: an integer vector, the number of false positives undirected edges.
 skel.fn: an integer vector, the number of false negatives undirected edges.
 order.fp: an integer vector, the number of false positive order relations.
 order.fn: an integer vector, the number of false negative order relations.
 markov.fp: an integer vector, the number of false positive Markov pairs.
 markov.fn: an integer vector, the number of false negative Markov pairs.
 KLdist: a numerical vector, the KL distance, currently inactive.
 time: a numerical, the processing time in seconds.

Methods

cnFind signature(object="catNetworkEvaluate", complexity="integer"): Finds a network in the list nets with specific complexity.

cnFindAIC signature(object="catNetworkEvaluate"): Finds the optimal network according to AIC criterion.

cnFindBIC signature(object="catNetworkEvaluate"): Finds the optimal network according to BIC criterion.

cnPlot signature(object="catNetworkEvaluate"): Draw distance plots.

Author(s)

N. Balov

See Also

[catNetwork-class](#), [catNetworkDistance-class](#), [cnCompare](#), [cnPlot](#)

classification

Classification demonstration

Description

Detailed information on the analysis can be found in our paper "Discrete Bayesian Network Classification for Gene Expression Data". From the installation catnet/demo directory copy the files cvK-for1.r, diabetesLoad.r, diabetes.r, bostonLoad.r and boston.r into a new directory along with the data files "Diabetes_collapsed_symbols.gct", "Lung_Michigan_collapsed_symbols.gct" and "Lung_Boston_collapsed_symbols.gct" beforehand downloaded from the GSEA site. Then call demo(diabetes) and demo(boston) or open the files and execute the code manually. The processing takes hours.

cnCatnetFromEdges	<i>catNetwork from Edges</i>
-------------------	------------------------------

Description

Creates a catNetwork object from list of nodes and edges.

Usage

```
cnCatnetFromEdges(nodes, edges, numCategories=2)
```

Arguments

nodes	a vector of node names
edges	a list of node edges
numCategories	an integer, the number of categories per node

Details

The function uses a list of nodes and directional edges to create a catNetwork with specified (fixed) number of node categories. A random probability model is assigned, which can be changed later by cnSetProb for example. Note that cnSetProb takes a given data sample and changes both the node categories and their conditional probabilities according to it.

Value

A catNetwork object

Author(s)

N. Balov

See Also

[cnNew](#), [cnCatnetFromSif](#), [cnSetProb](#)

cnCatnetFromSif	<i>Categorical Network from Simple Interaction File (SIF) and Bayesian Networks Interchange Format (BIF)</i>
-----------------	--------------------------------------------------------------------------------------------------------------

Description

Creates a catNetwork object from a SIF/BIF file.

Usage

```
cnCatnetFromSif(file, numcats=2)
cnCatnetFromBif(file)
```

Arguments

file	a file name
numcats	an integer, the number of node categories

Details

The function imports a graph structure from a SIF file by assigning equal number numcats of categories for each of its nodes and a random probability model. Subsequently, the probability model can be changed by calling cnSetProb function.

Value

A catNetwork object

Author(s)

N. Balov

See Also

[cnNew](#), [cnCatnetFromEdges](#), [cnSetProb](#)

cnCluster-method *Network Clustering*

Description

Retrieving the clusters, the connected sub-networks, of a given network. Estimating the clusters from data.

Usage

```
cnCluster(object)
cnClusterSep(object, data, perturbations=NULL)
cnClusterMI(data, perturbations=NULL, threshold=0)
```

Arguments

object	a catNetwork
data	a matrix in row-nodes format or a data.frame in column-nodes format
perturbations	a binary perturbation matrix with the dimensions of data
threshold	a numeric value

Details

The function `cnCluster` constructs a list of subsets of nodes of the object, each representing a connected sub-network. Isolated nodes, these are nodes not connected to any other, are not reported. Thus, every element of the output list contains at least two nodes. The function `cnClusterMI` clusters the nodes of the data using the pairwise mutual information and critical value threshold.

Value

A list of named nodes.

Author(s)

N. Balov

Examples

```
cnet <- cnRandomCatnet(numnodes=30, maxParents=2, numCategories=2)
cnCluster(object=cnet)
```

cnCompare-method *Network Comparison*

Description

Compares two catNetwork objects by several criteria

Usage

```
cnCompare(object1, object2, extended = TRUE)
```

Arguments

object1	a catNetwork object
object2	a catNetwork object, matrix, list of catNetworks or catNetworkEvaluate object
extended	a logical parameter, specifying whether basic but quicker or extended comparison to be performed

Details

Comparison can be performed only between networks with the same sets of nodes. The function considers several topology-related comparison metrics.

First, directed edge comparison is performed and the true positives (TP), the false positive (FP) and the false negatives (FN) are reported assuming object1 to be the 'true' network.

Second, the difference between the binary parent matrices of the two objects is measured as the number of positions at which they differ. This is the so called Hamming distance and it is coded as hamm. Also, when extended parameter is set to TRUE, the difference between the exponents of the parent matrices is calculated, hammexp.

Third, the node order difference between the two networks is measured as follows. Let us call 'order pair' a pair of indices (i,j) such that there is a directed path from j-th node to i-th node in the network, which sometimes is denoted by $j > i$. The order comparison is done by counting the false positive and false negative order pairs.

The fourth criteria accounts for the so called 'Markov blanket'. The term 'Markov pair' is used to denote a pair of indices which corresponding nodes have a common child. In case of extended comparison, the numbers of false positive and false negative Markov pairs are calculated.

The cnCompare function returns an object with the following slots: 1) the number of true positive edges TP; 2) the number of false positive edges FP; 3) the number of false negative edges FN; 4) the F-score, which is the harmonic average of the specificity and sensitivity 5) the number of different elements in the corresponding parent matrices hamm; 6) the total number of different elements between all powers of the parent matrices hammexp;

Next three numbers identify the difference in the objects' skeletons (undirected graph structure)

7) the number of true positive undirected edges TP; 8) the number of false positive undirected edges FP; 9) the number of false negative undirected edges FN;

10) the number of false positive order pairs `order.fp`; 11) the number of false negative order pairs `order.fn`; 12) the number of false positive Markov pairs `markov.fp`; and 13) the number of false positive Markov pairs `markov.fn`. It is assumed that the first object represents the ground truth with respect to which the comparison is performed.

If `extended` is set off (FALSE) only the edge (TP, FP, FN) and skeleton (TP, FP, FN) numbers are reported, otherwise all distance parameters are calculated. Turning off the `extended` option is recommended for very large networks (e.g. with number of nodes > 500), since the calculation of some of the distance metrics involve matrix calculations for which the function is not optimized and can be very slow.

Value

A `catNetworkDistance` if `object2` is `catNetwork` and `catNetworkEvaluate` otherwise.

Author(s)

N. Balov

See Also

[catNetworkEvaluate-class](#)

Examples

```
cnet1 <- cnRandomCatnet(numnodes=10, maxParents=2, numCategories=2)
cnet2 <- cnRandomCatnet(numnodes=10, maxParents=2, numCategories=2)
dist <- cnCompare(object1=cnet1, object2=cnet2)
dist
```

cnComplexity-method *Network Complexity*

Description

Returns the complexity of a network

Usage

```
cnComplexity(object, node=NULL, include.unif=TRUE)
cnKLCplexity(object, node=NULL)
```

Arguments

<code>object</code>	a <code>catNetwork</code> object
<code>node</code>	an integer, node index
<code>include.unif</code>	a logical

Details

Complexity is a network characteristics that depends both on its graphical structure and the categorization of its nodes.

If node is specified, then the function returns that node complexity, otherwise the total complexity of object, which is the sum of its node complexities, is reported. A node complexity is determined by the number of its parents and their categories. For example, a node without parents has complexity 1. A node with k parents with respected number of categories c_1, c_2, \dots, c_k , has complexity $c_1 * c_2 * \dots * c_k$. Complexity is always a number that is equal or greater than the number of nodes in the network. For a network with specified graph structure, its complexity determines the number of parameters needed to define its probability distribution and hence the importance of complexity as network characteristic.

If `include.unif` is set to `FALSE`

Value

An integer

Author(s)

N. Balov, P. Salzman

Examples

```
library(catnet)
cnet <- cnRandomCatnet(numnodes=10, maxParents=3, numCategories=2)
cnComplexity(object=cnet)
```

cnDiscretize

Data Categorization

Description

Numerical data discretization using empirical quantiles.

Usage

```
cnDiscretize(data, numCategories, mode="uniform", qllevels=NULL)
```

Arguments

<code>data</code>	a numerical matrix or <code>data.frame</code>
<code>numCategories</code>	an integer, the number of categories per node
<code>mode</code>	a character, the discretization method to be used, "quantile" or "uniform"
<code>qllevels</code>	a list of integer vectors, the node discretization parameters

Details

The numerical data is discretized into given number of categories, `numCategories`, using the empirical node quantiles. As in all functions of `catnet` package that accept data, if the `data` parameter is a `matrix` then it is organized in the row-node format. If it is a `data.frame`, the column-node format is assumed.

The `mode` specifies the discretization model. Currently, two discretization methods are supported - "quantile" and "uniform", which is the default choice.

The quantile-based discretization method is applied as follows. For each node, the sample node distribution is constructed, which is then represented by a sum of non-intersecting classes separated by the quantile points of the sample distribution. Each node value is assigned the class index in which it falls into.

The uniform discretization breaks the range of values of each node into `numCategories` equal intervals or of lengths proportional to the corresponding `qlevels` values.

Currently, the function assigns equal number of categories for each node of the data.

Value

A `matrix` or `data.frame` of indices.

Author(s)

N. Balov, P. Salzman

See Also

[cnSamples](#)

Examples

```
ps <- t(sapply(1:10, function(i) rnorm(20, i, 0.1)))
dps1 <- cnDiscretize(ps, 3, mode="quantile")
hist(dps1[1,])
qlevels <- lapply(1:10, function(i) rep(1, 3))
qlevels[[1]] <- c(1,2,1)
dps2 <- cnDiscretize(ps, 3, mode="uniform", qlevels)
hist(dps2[1,])
```

cnDot-method

Network Description File

Description

The function generates a dot-file, the native storage format for Graphviz software package, that describes the graph structure of a `catNetwork` object.

Usage

```
cnDot(object, file=NULL, format="ps", style=NULL)
```

Arguments

object	a catNetwork, a list of catNetworks or a parent matrix
file	a character, an optional output file name
format	a character, an optional output file format, "ps" or "pdf"
style	a list of triplets, nodes' shape, color and edge-color

Details

The function generates a dot-text file as supported by Graphviz library. In order to draw a graph the user needs a dot-file converter and pdf/postscript viewer. The environment variables R_DOTVIEWER and R_PDFVIEWER specify the corresponding executable routines.

If Graphviz is installed and the variable R_DOTVIEWER is set with the full path to the dot executable file (the routine that converts a dot-text file to a postscript or pdf), a pdf or postscript file is created depending on the value of the format parameter.

If the file variable is not specified, then the function just prints out the resulting string which otherwise would be written into a dot file. Next, if a pdf-viewer is available, the created postscript or pdf file is shown.

Value

A character or a dot-file

Author(s)

N. Balov

See Also

[catnet-package](#), [cnPlot](#)

Examples

```
cnet <- cnRandomCatnet(numnodes=10, maxParents=3, numCategories=2)
cnDot(object=cnet, file="cnet")
```

`cnEdges-method`*Network Edges*

Description

Returns the set of directed edges of a `catNetwork` object.

Usage

```
cnEdges(object, which)
```

Arguments

<code>object</code>	a <code>catNetwork</code>
<code>which</code>	a vector of node indices or node names

Details

The edges of a `catNetwork` are specified as parent-to-child vectors. The function returns a list that for each node with index in the vector `which` contains its set of children. If `which` is not specified, the children of all nodes are listed.

Value

A list of nodes' children.

Author(s)

N. Balov, P. Salzman

See Also

[cnParents](#)

Examples

```
library(catnet)
cnet <- cnRandomCatnet(numnodes=10, maxParents=3, numCategories=2)
cnEdges(object=cnet)
```

cnEntropy	<i>Pairwise Node Entropy</i>
-----------	------------------------------

Description

Calculates the matrix of conditional entropy for each pair of nodes.

Usage

```
cnEntropy(data, perturbations=NULL)
cnEdgeDistanceKL(data, perturbations)
cnEdgeDistancePearson(data, perturbations)
cnEntropyOrder(data, perturbations=NULL)
```

Arguments

data	a matrix in row-nodes format or a data.frame in column-nodes format
perturbations	a binary matrix with the dimensions of data. A value 1 designates the corresponding node in the sample as perturbed.

Details

The conditional entropy of node X with respect to Y is defined as $-P(X|Y)\log P(X|Y)$, where $P(X|Y)$ is the sample conditional probability, and this is the value at the (X,Y) 'th position in the resulting matrix.

Value

A matrix

Author(s)

N. Balov

See Also

[cnParHist](#)

cnFind-method	<i>Find Network by Complexity</i>
---------------	-----------------------------------

Description

This is a model selection routine that finds a network in a set of networks for a given complexity.

Usage

```
cnFind(object, complexity = 0, alpha=0, factor=1)
cnFindKL(object, numsamples)
```

Arguments

object	catNetworkEvaluate or list of catNetworks
complexity	an integer, target complexity
alpha	a character or numeric
factor	a numeric
numsamples	an integer

Details

The complexity must be at least the number of nodes of the networks. If no network with the requested complexity exists in the list, then the one with the closest complexity is returned. Alternatively, one can apply some standard model selection with `alpha="BIC"` and `alpha=AIC`.

Value

A catNetwork object.

Author(s)

N. Balov, P. Salzman

See Also

[cnFindAIC](#), [cnFindBIC](#)

Examples

```
cnet <- cnRandomCatnet(numnodes=10, maxParents=2, numCategories=2)
psamples <- cnSamples(object=cnet, numsamples=100)
netlist <- cnSearchOrder(data=psamples, maxParentSet=2)
bnet <- cnFind(object=netlist, complexity=cnComplexity(cnet))
bnet
```

cnFindAIC-method	<i>Find Network by AIC</i>
------------------	----------------------------

Description

This is a model selection routine that finds a network in a set of networks using the AIC criteria.

Usage

```
cnFindAIC(object, numsamples)
```

Arguments

object	A list of catNetwork objects or catNetworkEvaluate
numsamples	an integer

Details

The function returns the network with maximal AIC value from a list of networks as obtained from one of the search-functions `cnSearchOrder`, `cnSearchSA` and `cnSearchSAcluster`. The formula used for the AIC is $\log(\text{Likelihood}) - \text{Complexity}$.

Value

A catNetwork object with optimal AIC value.

Author(s)

N. Balov, P. Salzman

See Also

[cnFind](#), [cnFindBIC](#)

Examples

```
library(catnet)
cnet <- cnRandomCatnet(numnodes=12, maxParents=3, numCategories=2)
psamples <- cnSamples(object=cnet, numsamples=10)
nodeOrder <- sample(1:12)
nets <- cnSearchOrder(data=psamples, perturbations=NULL,
maxParentSet=2, maxComplexity=36, nodeOrder)
aicnet <- cnFindAIC(object=nets)
aicnet
```

cnFindBIC-method *Find Network by BIC*

Description

This is a model selection routine that finds a network in a set of networks using the BIC criteria.

Usage

```
cnFindBIC(object, numsamples)
```

Arguments

object	A list of catNetworkNode objects or catNetworkEvaluate
numsamples	The number of samples used for estimating object

Details

The function returns the network with maximal BIC value from a list of networks as obtained from one of the search-functions `cnSearchOrder`, `cnSearchSA` and `cnSearchSAcluster`. The formula used for the BIC is $\log(\text{Likelihood}) - 0.5 * \text{Complexity} * \log(\text{numNodes})$.

Value

A catNetwork object with optimal BIC value.

Author(s)

N. Balov, P. Salzman

See Also

[cnFindAIC](#), [cnFind](#)

Examples

```
library(catnet)
cnet <- cnRandomCatnet(numnodes=12, maxParents=3, numCategories=2)
psamples <- cnSamples(object=cnet, numsamples=10)
nodeOrder <- sample(1:12)
nets <- cnSearchOrder(data=psamples, perturbations=NULL,
maxParentSet=2, maxComplexity=36, nodeOrder)
bicnet <- cnFindBIC(object=nets, numsamples=dim(psamples)[2])
bicnet
```

cnLoglik-method	<i>Sample Log-likelihood</i>
-----------------	------------------------------

Description

Calculate the log-likelihood of a sample with respect to a given catNetwork object

Usage

```
cnLoglik(object, data, perturbations=NULL, bysample=FALSE)
```

Arguments

object	a catNetwork object
data	a data matrix given in the column-sample format, or a data.frame in the row-sample format
perturbations	a binary matrix with the dimensions of data. A value 1 designates the corresponding node in the sample as perturbed.
bysample	a logical

Details

If bysample is set to TRUE, the function output is a vector of log-likelihoods of the individual sample records. Otherwise, the total average of the log-likelihood of the sample is reported.

Value

A numeric value

Author(s)

N. Balov

See Also

[cnNodeLoglik](#)

Examples

```
library(catnet)
cnet <- cnRandomCatnet(numnodes=10, maxParents = 3, numCategories = 2)
psamples <- cnSamples(object=cnet, numsamples=100)
cnLoglik(object=cnet, data=psamples)
```

cnMatEdges-method *Network Edge Matrix*

Description

Returns a matrix representing the edges of a catNetwork object.

Usage

```
cnMatEdges(object)
```

Arguments

object a catNetwork object

Details

The resulting matrix has two columns and the number of edges rows. Edges are given as ordered pairs of the elements of the first and second columns.

Value

A matrix of characters.

Author(s)

N. Balov, P. Salzman

See Also

[cnEdges](#), [cnMatParents](#)

Examples

```
library(catnet)
cnet <- cnRandomCatnet(numnodes=10, maxParents=3, numCategories=2)
cnMatEdges(object=cnet)
```

cnMatParents-method *Network Parent Matrix*

Description

Returns the binary matrix of parent-child relations of a `catNetwork` object.

Usage

```
cnMatParents(object, nodeorder)
```

Arguments

`object` a `catNetwork` or `catNetworkFit` object
`nodeorder` an integer vector specifying the order of the nodes to be taken

Details

The resulting matrix has a value 1 at row *i* and column *j* if *i*-th node has *j*-th node as a parent, and 0 otherwise.

Value

A matrix

Author(s)

N. Balov, P. Salzman

See Also

[cnParents](#), [cnMatEdges](#)

Examples

```
library(catnet)
cnet <- cnRandomCatnet(numnodes=10, maxParents=3, numCategories=2)
cnMatParents(object=cnet)
```

`cnNew`*New catNetwork*

Description

Creates a new `catNetwork` with specified nodes, categories, parent sets and probability structure.

Usage

```
cnNew(nodes, cats, parents, probs=NULL, p.delta1=0.01, p.delta2=0.01)
```

Arguments

<code>nodes</code>	a vector of nodes names
<code>cats</code>	a list of node categories
<code>parents</code>	a list of node parents
<code>probs</code>	a list of probabilities
<code>p.delta1</code>	a numeric
<code>p.delta2</code>	a numeric

Details

If `probs` is not specified, then a random probability model is assigned with conditional probability values in the union of the intervals $[p.\text{delta}1, 0.5-p.\text{delta}2]$ and $[0.5+p.\text{delta}2, 1-p.\text{delta}1]$. Because of the nested list hierarchy of the probability structure, specifying the probability argument explicitly can be very elaborated task for large networks. In the following example we create a small network with only three nodes. The first node has no parents and only its marginal distribution is given, $c(0.2, 0.8)$. Note that all inner most vectors in the `probs` argument, such as $(0.4, 0.6)$, represent conditional distributions and thus sum to 1.

Value

A `catNetwork` object.

Author(s)

N. Balov, P. Salzman

See Also

[catNetwork-class](#), [cnRandomCatnet](#)

Examples

```

library(catnet)
cnet <- cnNew(
  nodes = c("a", "b", "c"),
  cats = list(c("1", "2"), c("1", "2"), c("1", "2")),
  parents = list(NULL, c(1), c(1, 2)),
  probs = list( c(0.2, 0.8),
    list(c(0.6, 0.4), c(0.4, 0.6)),
    list(list(c(0.3, 0.7), c(0.7, 0.3)),
      list(c(0.9, 0.1), c(0.1, 0.9))))
)

```

cnNodeLoglik

Node Log-likelihood

Description

For a given data sample, the function calculates the log-likelihood of a node with respect to a specified parent set.

Usage

```
cnNodeLoglik(object, node, data, perturbations=NULL)
```

Arguments

object	a catNetwork object
node	an integer or a list of integers, node indices in the data
data	a matrix or data.frame of categories
perturbations	an optional perturbation matrix or data.frame

Value

a numeric value

Author(s)

N. Balov

See Also

[cnLoglik](#)

Examples

```

library(catnet)
cnet <- cnRandomCatnet(numnodes=10, maxParents=3, numCategories=2)
psamples <- cnSamples(object=cnet, numsamples=100)
cnNodeLoglik(cnet, node=5, data=psamples)

```

cnNodeMarginalProb-method

Probability Calculations

Description

Marginal probability of a node, joint probability of a set of nodes or conditional probability of two sets of nodes.

Usage

```
cnNodeMarginalProb(object, node)
cnJointProb(object, nodes)
cnCondProb(object, x, y)
```

Arguments

object	a catNetwork
node	an integer, a node index in object
nodes	a vector of node names or indices in object
x,y	vectors of node categories (either characters or indices) named after nodes of object

Details

cnJointProb returns a matrix with probability values for each combination of categories arranged in columns. cnCondProb calculates the value of $P(X=x|Y=y)$.

Value

a numerical or numerical matrix

Author(s)

N. Balov

See Also

[cnProb](#)

Examples

```
library(catnet)
cnet <- cnRandomCatnet(numnodes=10, maxParents=3, numCategories=2)
cnNodeMarginalProb(cnet, node=5)
cnCondProb(cnet, x=c("N1"=1, "N2"=2), y=c("N3"=1, "N4"=2, "N5"=2))
```

cnNodes-method	<i>Network Nodes</i>
----------------	----------------------

Description

Returns the list of nodes of a catNetwork object.

Usage

```
cnNodes(object, which)
```

Arguments

object	a catNetwork object
which	a vector of node indices

Details

Nodes are represented by characters. When a random catNetwork object is constructed, it takes the default node names N#, where # are node indices. The function returns the node names with indices given by parameter which, and all node names if which is not specified.

Value

a list of characters, the node names

Author(s)

N. Balov, P. Salzman

See Also

[cnNumNodes](#)

Examples

```
library(catnet)
cnet <- cnRandomCatnet(numnodes=10, maxParents=3, numCategories=2)
cnNodes(object=cnet)
```

cnNodeSampleLoglik *Node Log-likelihood*

Description

For a given data sample, the function calculates the log-likelihood of a node with respect to a specified parent set.

Usage

```
cnNodeSampleLoglik(node, parents, data, perturbations=NULL)
cnNodeSampleProb(node, parents, data, perturbations=NULL)
```

Arguments

node	an integer or a list of integers, node indices in the data
parents	an integer or a list of integers, vector of parent indices for the nodes
data	a matrix or data.frame of categories
perturbations	an optional perturbation matrix or data.frame

Value

a numeric value

Author(s)

N. Balov

See Also

[cnLoglik](#)

Examples

```
library(catnet)
cnet <- cnRandomCatnet(numnodes=10, maxParents=3, numCategories=2)
psamples <- cnSamples(object=cnet, numsamples=100)
cnNodeSampleLoglik(node=5, parents=c(1,2), data=psamples)
```

cnNumNodes-method *Network Size*

Description

Returns the number of nodes of a catNetwork object.

Usage

```
cnNumNodes(object)
```

Arguments

object a catNetwork

Value

an integer

Author(s)

N. Balov, P. Salzman

See Also

[cnNodes](#)

Examples

```
library(catnet)
cnet <- cnRandomCatnet(numnodes=10, maxParents=3, numCategories=2)
cnNumNodes(object=cnet)
```

cnOrder-method *Network Node Order*

Description

The function returns an order of the nodes of a network that is compatible with its parent structure.

Usage

```
cnOrder(object)
```

Arguments

object a catNetwork or a list of node parents.

Details

An order is compatible with the parent structure of a network if each node has as parents only nodes appearing earlier in that order. That such an order exists is guaranteed by the fact that every `catNetwork` is a DAG (Directed Acyclic Graph). The result is one order out of, eventually, many possible.

Value

a list of node indices.

Author(s)

N. Balov, P. Salzman

Examples

```
cnet <- cnRandomCatnet(numnodes=20, maxParents=3, numCategories=2)
cnOrder(object=cnet)
```

cnParents-method	<i>Network Parent Structure</i>
------------------	---------------------------------

Description

Returns the list of parents of selected nodes of a `catNetwork` object. If `which` is not specified, the parents of all nodes are listed.

Usage

```
cnParents(object, which)
```

Arguments

<code>object</code>	a <code>catNetwork</code> object
<code>which</code>	a vector of node indices

Value

A list of named nodes.

Author(s)

N. Balov, P. Salzman

See Also

[cnMatParents](#), [cnEdges](#)

Examples

```
library(catnet)
cnet <- cnRandomCatnet(numnodes=10, maxParents=3, numCategories=2)
cnParents(object=cnet)
```

cnParHist-method *Parenthood Histogram*

Description

Calculates the histogram of parent-child edges for a `catNetworkEvaluate` object or a list of `catNetwork`s

Usage

```
cnParHist(object)
```

Arguments

`object` `catNetworkEvaluate` or list of `catNetwork` objects

Value

a numerical matrix

Author(s)

N. Balov, P. Salzman

Examples

```
cnet <- cnRandomCatnet(numnodes=20, maxParents=3, numCategories=2)
psamples <- cnSamples(cnet, 100)
nodeOrder <- sample(1:20)
nets <- cnSearchOrder(psamples, perturbations=NULL,
maxParentSet=2, maxComplexity=50, nodeOrder)
cnParHist(object=nets)
```

cnPearsonTest-method *Goodness of Fit Test*

Description

The function calculates the Pearson's chi-square statistics for all nodes of a network.

Usage

```
cnPearsonTest(object, data)
```

Arguments

object	a catNetwork
data	a data matrix or data.frame

Details

For given data and network object, the function reports both the chi-square statistics and the degree of freedom for each node in the network for the purpose of performing goodness of fit tests.

Value

A list

Author(s)

N. Balov

cnPlot-method *Plot Network*

Description

Draws the graph structure of catNetwork object or some diagnostic plots associated with a catNetworkEvaluate

Usage

```
cnPlot(object, file=NULL)
```

Arguments

object	catNetwork or catNetworkEvaluate object
file	a file name

Details

First we consider the case when object is a catNetwork. There are two visualization options implemented - one using 'igraph' and the other 'Graphviz'. The usage of these two alternatives is controlled by two environment variables - the logical one R_CATNET_USE_IGRAPH and the character one R_DOTVIEWER, correspondingly. If igraph is installed and R_CATNET_USE_IGRAPH is set to TRUE, the function constructs an igraph compatible object corresponding to the object and plot it.

If igraph is not found, the function generates a dot-file with name file.dot, if file is specified, or unknown.dot otherwise. Furthermore, provided that Graphviz library is found and R_DOTVIEWER points to the dot-file executable, the created earlier dot-file will be compiled to pdf or postscript, if object is a list. Finally, if the system has pdf or postscript rendering capabilities and R_PDFVIEWER variable shows the path to the pdf-rendering application, the resulting pdf-file will be shown.

In case object is of class catNetworkEvaluate, then the function draws six relevant plots: likelihood vs. complexity, Hamming (hamm) and exponential Hamming (hammexp) distances, Markov neighbor distance (FP plus FN), and the false positive (fp) and false negative (fn) edges vs. complexity.

Value

A R-plot or dot-file or pdf-file.

Author(s)

N. Balov

See Also

[cnDot](#), [catNetworkEvaluate-class](#), [cnCompare](#)

Examples

```
## Set R_CATNET_USE_IGRAPH to TRUE if you want to use 'igraph'  
Sys.setenv(R_CATNET_USE_IGRAPH=FALSE)  
cnet <- cnRandomCatnet(numnodes=10, maxParents=3, numCategories=2)  
cnPlot(object=cnet)
```

cnPredict-method

Prediction

Description

Predicts the 'not-available' elements in an incomplete sample.

Usage

```
cnPredict(object, data)
```

Arguments

object a catNetwork
 data a data matrix or data.frame

Details

Data should be a matrix or data frame of categorical values or indices. If it is a matrix then the rows should represent object's nodes; otherwise, the columns represent the nodes. Data's values represent object's categories either as characters or indices. Indices should be integers in the range from 1 to the number of categories of the corresponding node. Prediction is made for those nodes that are marked as not-available (NA) in the data and is based on maximum probability criterion. For each data instance, the nodes are traversed in their topological order in object and the categorical values with the maximum probability are assigned.

Value

An updated sample matrix

Author(s)

N. Balov, P. Salzman

Examples

```
cnet <- cnRandomCatnet(numnodes=10, maxParents=3, numCategories=3)
## generate a sample of size 2 and set nodes 8, 9 and 10 as not-available
psamples <- matrix(as.integer(1+rbinom(10*2, 2, 0.4)), nrow=10)
psamples[8, ] <- rep(NA, 2)
psamples[9, ] <- rep(NA, 2)
psamples[10, ] <- rep(NA, 2)
## make show sample rows are named after the network's nodes
rownames(psamples) <- cnNodes(cnet)
## predict the values of nodes 8, 9 and 10
newsamples <- cnPredict(object=cnet, data=psamples)
```

 cnProb-method

Conditional Probability Structure

Description

Returns the list of conditional probabilities of nodes specified by which parameter of a catNetwork object. Node probabilities are reported in the following format. First, node name and its parents are given, then a list of probability values corresponding to all combination of parent categories (put in brackets) and node categories. For example, the conditional probability of a node with two parents, such that both the node and its parents have three categories, is given by 27 values, one for each of the 3*3*3 combination.

Usage

```
cnProb(object, which=NULL)
cnPlotProb(object, which=NULL)
```

Arguments

object	a catNetwork object
which	a vector of indices

Value

A named list of probability tables.

Author(s)

N. Balov, P. Salzman

Examples

```
library(catnet)
cnet <- cnRandomCatnet(numnodes=10, maxParents=3, numCategories=2)
cnProb(object=cnet)
cnPlotProb(object=cnet)
```

cnRandomCatnet	<i>Random Network</i>
----------------	-----------------------

Description

Creates a random catNetwork with specified number of nodes, number of parents and categories per node.

Usage

```
cnRandomCatnet(numnodes, maxParents, numCategories, p.delta1=0.01, p.delta2=0.01)
```

Arguments

numnodes	an integer, the number of nodes
maxParents	an integer, the maximum number of parents per node
numCategories	an integer, the number of categories for each node. It is the function limitation to support only constant number of node categories.
p.delta1	a numeric
p.delta2	a numeric

Details

A random set of parents, no more than `maxParents`, is assigned to each node along with a random conditional probability distribution with values in the union of $[p.\text{delta}1, 0.5-p.\text{delta}2]$ and $[0.5+p.\text{delta}2, 1-p.\text{delta}1]$. Also, each node is assigned a fixed, thus equal, number of categories, `numCategories`.

The function is designed for evaluation and testing purposes only thus lacking much user control over the networks it create. Once created with `cnRandomCatnet`, a network can be further modified manually node by node. However, this requires direct manipulation of the object's slots and may result in a wrong network object. It is recommended that after any manual manipulation a call `is(object, "catNetwork")` is performed to check the object's integrity.

Value

A `catNetwork` object

Author(s)

N. Balov

See Also

[cnNew](#)

Examples

```
cnet <- cnRandomCatnet(numnodes=20, maxParents=3, numCategories=2)
```

cnReorderNodes-method *Reorder Network Nodes*

Description

The function rearranges the nodes of a network according to a new order.

Usage

```
cnReorderNodes(object, nodeIndices)
```

Arguments

<code>object</code>	a <code>catNetwork</code>
<code>nodeIndices</code>	a vector representing the new node order

Details

Node reordering affects the list of node names, parents and probabilities. It is a useful operation in cases when comparison of two networks is needed.

Value

A catNetwork object.

Author(s)

N. Balov, P. Salzman

Examples

```

cnet <- cnRandomCatnet(numnodes=10, maxParents=3, numCategories=2)
cnMatParents(cnet)
cnet1 <- cnReorderNodes(object=cnet, nodeIndices=cnOrder(cnet))
cnNodes(object=cnet1)
cnMatParents(cnet1)

```

cnSamples-method *Samples from Network*

Description

Generates samples from of a catNetwork object.

Usage

```

cnSamples(object, numsamples = 1, perturbations = NULL, output="frame",
as.index=FALSE, naRate=0)

```

Arguments

object	a catNetwork
numsamples	an integer, the number of samples to be generated
perturbations	a vector, node perturbations
output	a character, the output format. Can be a data.frame or matrix.
as.index	a logical, the output categorical format
naRate	a numeric, the proportion of NAs per sample instance

Details

If the output format is "matrix" then the resulting sample matrix is in row-node format - the rows correspond to the object's nodes while the individual samples are represented by columns. If the output format is "frame", which is by default, the result is a data frame with columns representing the nodes and levels the set of categories of the respected nodes. If `as.index` is set to `TRUE`, the output sample consists of categorical indices, otherwise, and this is by default, of characters specifying the categories.

A perturbed sample is a sample having nodes with predefined, thus fixed, values. Non-perturbed nodes, the nodes which values have to be set, are designated with zeros in the perturbation vector

and their values are generated conditional on the values of their parents. While the non-zero values in the perturbation vector are carried on unchanged to the output.

If naRate is positive, then `floor(numnodes*naRate)` NA values are randomly placed in each sample instance.

Value

A matrix or data.frame of node categories as integers or characters

Author(s)

N. Balov

See Also

[cnPredict](#)

Examples

```
cnet <- cnRandomCatnet(numnodes=10, maxParents=3, numCategories=3)
## generate a sample of size 100 from cnet
psamples <- cnSamples(object=cnet, numsamples=100, output="frame", as.index=FALSE)
## perturbed sample
nsamples <- 20
perturbations <- rbinom(10, 2, 0.4)
## generate a perturbed sample of size 100 from cnet
psamples <- cnSamples(object=cnet, numsamples=nsamples, perturbations, as.index=TRUE)
```

cnSearchHist

Parent Histogram Matrix

Description

Estimation of the parent matrix of nodes from data. The frequency of node edges is obtained by fitting networks consistent to randomly generated node orders.

Usage

```
cnSearchHist(data, perturbations=NULL,
maxParentSet=1, parentSizes=NULL, maxComplexity=0,
nodeCats=NULL, parentsPool=NULL, fixedParents=NULL,
score = "BIC", weight="likelihood",
maxIter=32, numThreads=2, echo=FALSE)
```


Arguments

data	a matrix in row-nodes format or a data.frame in column-nodes format
perturbations	a binary matrix with the dimensions of data. A value 1 designates the corresponding node in the sample as perturbed
maxParentSet	an integer, the maximal number of parents per node
parentsSizes	an integer vector, maximal number of parents per node
maxComplexity	an integer, the maximal network complexity for the search
nodeCats	a list of node categories
parentsPool	a list of parent sets to choose from
fixedParents	a list of parent sets to choose from
score	a character, network selection score such as "AIC" and "BIC"
weight	a character, specifies how the
maxIter	an integer, the number of single order searches to be performed
numThreads	an integer value, the number of parallel threads
echo	a boolean that sets on/off some functional progress and debug information

Details

The function performs `niter` calls of `cnSearchOrder` for randomly generated node orders (uniformly over the space of all possible node orders), selects networks according to `score` and sum their parent matrices weighted by `weight`. Three scoring criteria are currently supported: "BIC", "AIC" and maximum complexity for any other value of `score`. The `weight` can be 1) "likelihood", then the parent matrices are multiplied by the network likelihood, 1) "score", then the parent matrices are multiplied by the exponential of the network score, 3) any other value of `weight` uses multiplier 1. In this case the entries in the output matrix show how many times the corresponding parent-child pairs were found.

The function can runs `numThreads` number of parallel threads each processing different order. `cnSearchHist` function can be useful for empirical estimation of the relationships in some multivariate categorical data.

Value

A matrix

Author(s)

N. Balov

See Also

[cnMatParents](#), [cnSearchOrder](#)

Examples

```

cnet <- cnRandomCatnet(numnodes=8, maxParents=3, numCategories=2)
psamples <- cnSamples(object=cnet, numsamples=100)
mhisto <- cnSearchHist(data=psamples, perturbations=NULL,
maxParentSet=2, maxComplexity=20)
mhisto

```

cnSearchOrder

Network Search for Given Node Order

Description

The function implements a MLE based algorithm to search for optimal networks complying with a given node order. It returns a list of networks, with complexities up to some maximal value, that best fit the data.

Usage

```

cnSearchOrder(data, perturbations=NULL,
maxParentSet=0, parentSizes=NULL, maxComplexity=0,
nodeOrder=NULL,
nodeCats=NULL, parentsPool=NULL, fixedParents=NULL, edgeProb=NULL,
echo=FALSE)

```

Arguments

data	a matrix in row-nodes format or a data.frame in column-nodes format
perturbations	a binary matrix with the dimensions of data. A value 1 marks that the node in the corresponding sample as perturbed
maxParentSet	an integer, maximal number of parents for all nodes
parentSizes	an integer vector, maximal number of parents per node
maxComplexity	an integer, the maximal network complexity for the search
nodeOrder	a vector specifying a node order; the search is among the networks consistent with this topological order
nodeCats	a list of node categories
parentsPool	a list of parent sets to choose from
fixedParents	a list of parent sets to choose from
edgeProb	a square matrix of length the number of nodes specifying prior edge probabilities
echo	a logical that sets on/off some functional progress and debug information

Details

The data can be a matrix of character categories with rows specifying the node-variables and columns assumed to be independent samples from an unknown network, or a `data.frame` with columns specifying the nodes and rows being the samples.

The number of node categories are obtained from the sample. If given, the `nodeCats` is used as a list of categories. In that case, `nodeCats` should include the node categories presented in the data.

The function returns a list of networks, one for each admissible complexity within the specified range. The networks in the list are the Maximum Likelihood estimates in the class of networks having the given topological order of the nodes and complexity. When `maxComplexity` is not given, thus zero, its value is reset to the maximum possible complexity for the given parent set size. When `nodeOrder` is not given or `NULL`, the order of the nodes in the data is taken, `1, 2, . . .`

The parameters `parentsPool` and `fixedParents` allow the user to put some exclusion/inclusion constraints on the possible parenthood of the nodes. They should be given as lists of index vectors, one for each node.

The rows in `edgeProb` correspond to the nodes in the sample. The `[i,j]`-th element in `edgeProb` specifies a prior probability for the `j`-th node to be a parent of the `i`-th one. In calculating the prior probability of a network all edges are assumed independent Bernoulli random variables. The elements of `edgeProb` are cropped in the range `[0,1]`, such that the zero probabilities effectively exclude the corresponding edges, while the ones force them.

Value

A `catNetworkEvaluate` object

Author(s)

N. Balov, P. Salzman

See Also

[cnSearchSA](#)

Examples

```
cnet <- cnRandomCatnet(numnodes=12, maxParents=3, numCategories=2)
psamples <- cnSamples(object=cnet, numsamples=100)
nodeOrder <- sample(1:12)
nets <- cnSearchOrder(data=psamples, perturbations=NULL,
maxParentSet=2, maxComplexity=36, nodeOrder)
## next we find the network with complexity of the original one and plot it
cc <- cnComplexity(object=cnet)
cnFind(object=nets, complexity=cc)
```

cnSearchSA

*Stochastic Network Search***Description**

This function provides a MLE based network search in the space of node orders by Simulated Annealing. For a given sample from an unknown categorical network, it returns a list of `catNetwork` objects, with complexity up to some maximal value, that best fit the data.

Usage

```
cnSearchSA(data, perturbations,
maxParentSet=0, parentSizes=NULL,
maxComplexity=0, nodeCats=NULL,
parentsPool=NULL, fixedParents=NULL,
edgeProb=NULL, dirProb=NULL,
selectMode = "BIC",
tempStart=1, tempCoolFact=0.9, tempCheckOrders=10, maxIter=100,
orderShuffles=1, stopDiff=0,
numThreads=2, priorSearch=NULL, echo=FALSE)
```

Arguments

<code>data</code>	a matrix in row-nodes format or a <code>data.frame</code> in column-nodes format
<code>perturbations</code>	a binary matrix with the dimensions of <code>data</code> . A value 1 designates the node in the corresponding sample as perturbed
<code>maxParentSet</code>	an integer, maximal number of parents for all nodes
<code>parentSizes</code>	an integer vector, maximal number of parents per node
<code>maxComplexity</code>	an integer, maximal network complexity for the search
<code>nodeCats</code>	a list of node categories
<code>parentsPool</code>	a list of parent sets to choose from
<code>fixedParents</code>	a list of fixed parent sets
<code>edgeProb</code>	a square matrix of length the number of nodes specifying prior edge probabilities
<code>dirProb</code>	a square matrix of length the number of nodes specifying prior directional probabilities
<code>selectMode</code>	a character, optimization network selection criterion such as "AIC" and "BIC"
<code>tempStart</code>	a numeric value, the initial temperature for the annealing
<code>tempCoolFact</code>	a numeric value, the temperature multiplicative decreasing factor
<code>tempCheckOrders</code>	an integer, the number of iteration, orders to be searched, with constant temperature
<code>maxIter</code>	an integer, the total number of iterations, thus orders, to be processed

orderShuffles	a numeric, the number of shuffles for generating new candidate orders from the last accepted
stopDiff	a numeric value, stopping epsilon criterion
numThreads	an integer value, the number of parallel threads
priorSearch	a catNetworkEvaluate object from a previous search
echo	a logical that sets on/off some functional progress and debug information

Details

The function implements a Simulated Annealing version of the Metropolis algorithm by constructing a Markov chain in the space of node orders. Given a currently selected order, the algorithm tries to improve its likelihood score by exploring its neighborhood. The order score is defined as the likelihood of the selected according to selectMode network from the set of estimated networks compatible with that order.

The data can be a matrix of character categories with rows specifying the node-variables and columns assumed to be independent samples from an unknown network, or a data.frame with columns specifying the nodes and rows being the samples.

The number of categories for each node is obtained from the data. It is the user responsibility to make sure the data can be categorized reasonably. If the data is numerical it will be forcibly coerced to integer one, which however may result to NA entries or too many node categories per some nodes, and in either case to the function failure. Use cnDiscretize to convert numeric data into categorical. If given, the nodeCats is used as a list of categories. In that case, nodeCats should include the node categories presented in the data.

The function returns a list of networks, one for any possible complexity within the specified range. Stochastic optimization, based on the criterion of maximizing the likelihood, is carried on the network with complexity closest to, but not above, maxComplexity. If maxComplexity is not specified, thus the function is called with the default zero value, then maxComplexity is set to be the complexity of a network with all nodes having the maximum, maxParentSet, the number of parents. The selectMode parameter sets the selection criterion for the network upon which the maximum likelihood optimization is carried on. "BIC" is the default choice, while any value different from "AIC" and "BIC" results in the maximum complexity criterion to be used, the one which selects the network with complexity given by maxComplexity.

The parameters tempStart, tempCoolFact and tempCheckOrders control the Simulated Annealing schedule.

tempStart is the starting temperature of the annealing process.

tempCoolFact is the cooling factor from one temperature step to another. It is a number between 0 and 1, inclusively; For example, if tempStart is the temperature in the first step, tempStart*tempCoolFact will be temperature in the second.

tempCheckOrders is the number of proposals, that is, the candidate orders from the current order neighborhood, to be checked before decreasing the temperature. If for example maxIter is 40 and tempCheckOrders is 4, then 10 temperature decreasing steps will be eventually performed.

The orderShuffles parameters controls the extend of the current order neighborhood. A value of zero indicates that random orders should be used as proposals. For positive orderShuffles's, a candidate order is obtained from the current one by performing orderShuffles number of times the following operation: a random position is picked up at random (uniformly) and it is exchanged

with the position right up next to it. If `orderShuffles` is negative, then the operation is: two positions are picked up at random and their values are exchanged.

`maxIter` is the maximum length of the Markov chain.

`orderShuffles` is a number that controls the extent of the order neighborhoods. Each new proposed order is obtained from the last accepted one by `orderShuffles` switches of two node indices.

`stopDiff` is a stopping criterion. If at a current temperature, after `tempCheckOrders` orders being checked, no likelihood improvement of level at least `stopDiff` is found, then the SA stops and the function exists. Setting this parameter to zero guarantees exhausting all of the maximum allowed `maxIter` order searches.

The function speeds up the Markov Chain by implementing a pre-computing buffer. It runs `numThreads` number of parallel threads each of which process a proposed order. If we have more than one acceptance in the batch, the first one is taken as next order selection. The performance boost is more apparent when the Markov chain has a low acceptance rate, in which case the chain can run up to `numThreads`-times faster.

`priorSearch` is a result from previous search. This parameters allows a new search to be initiated from the best order found so far. Thus a chain of searches can be constructed with varying parameters providing greater adaptability and user control.

See the vignettes for more details on the algorithm.

Value

A `catNetworkEvaluate` object.

Author(s)

N. Balov, P. Salzman

See Also

[cnSearchOrder](#)

Examples

```
cnet <- cnRandomCatnet(numnodes=6, maxParents=2, numCategories=2)
psamples <- cnSamples(object=cnet, numsamples=100)
nets <- cnSearchSA(data=psamples, perturbations=NULL,
maxParentSet=1, maxComplexity=16)
cc <- cnComplexity(object=cnet)
cnFind(object=nets, complexity=cc)
```

cnSetProb-method *Set Probability from Data*

Description

The function sets the probability structure of a network from data according to the Maximum Likelihood criterion.

Usage

```
cnSetProb(object, data, perturbations=NULL, nodeCats=NULL)
```

Arguments

object	a catNetwork
data	a data matrix or data.frame
perturbations	a binary matrix with the dimensions of data
nodeCats	a list of node categories

Details

The function generates a new probability table for object and returns an updated catNetwork. The graph structure of the object is kept unchanged.

The data can be a matrix in the node-rows format, or a data.frame in the node-column format. If given, the nodeCats is used as a list of categories. In that case, nodeCats should include the node categories presented in the data.

Value

catNetwork

Author(s)

N. Balov

Examples

```
library(catnet)
cnet <- cnRandomCatnet(numnodes=10, maxParents=3, numCategories=3)
psamples <- matrix(as.integer(1+rbinom(10*100, 2, 0.4)), nrow=10)
rownames(psamples) <- cnet@nodes
newcnet <- cnSetProb(object=cnet, data=psamples)
```

cnSetSeed	<i>Random Generator Seed</i>
-----------	------------------------------

Description

Sets a seed for the random number generator.

Usage

```
cnSetSeed(seed)
```

Arguments

seed an integer

Details

Setting a fixed seed before any stochastic function guarantees repeated results.

Value

NA

Author(s)

N. Balov

cnSubNetwork-method	<i>Sub-Network</i>
---------------------	--------------------

Description

Returns a sub-network of a given catNetwork object.

Usage

```
cnSubNetwork(object, nodeIndices, indirectEdges)
```

Arguments

object a catNetwork
nodeIndices a vector, the subset of nodes to be taken
indirectEdges a logical, should the indirect connectivity be preserved

Details

The function creates a new network from a given one using a subset of its nodes, specified by `nodeIndices`. If `indirectIndices` is set to `TRUE`, then the resulting network contains edges between all nodes that are connected by chains of directed edges in the original one. The default value of `indirectIndices` is `FALSE`, thus the new set of edges is subset of the original one.

Value

A `catNetwork` object.

Author(s)

N. Balov

Examples

```
cnet <- cnRandomCatnet(numnodes=10, maxParents=3, numCategories=2)
cnet1 <- cnSubNetwork(object=cnet, nodeIndices=c(1,2,3,4,5), indirectEdges=TRUE)
cnNodes(object=cnet)
cnNodes(object=cnet1)
```

CPDAG-class

Class CPDAG

Description

Base class implementing Complete Partially Directed Acyclic Graphs (CPDAGs)

Slots

`numnodes`: an integer, the number of nodes

`nodes`: a vector of node names

`edges`: a list of graph edges

Author(s)

N. Balov

See Also

[dag2cpdag](#)

dag2cpdag-method	<i>Complete Network Representation</i>
------------------	----------------------------------------

Description

Generate the complete graphical structure for a catNetwork object.

Usage

```
dag2cpdag(object)
```

Arguments

object	a catNetwork object
--------	---------------------

Value

A non-DAG catNetwork object.

Author(s)

N. Balov

isDAG	<i>Check Direct Acyclic Graph (DAG) Condition</i>
-------	---------------------------------------------------

Description

For a pair of node and parent lists, the function checks whether the DAG condition holds or not.

Usage

```
isDAG(lnodes, lpars)
```

Arguments

lnodes	a list of nodes
lpars	a list of node parents

Details

The DAG verification algorithm is based on the topological ordering of the graph nodes. If node ordering is not possible, the graph is not a DAG.

Value

A logical TRUE/FALSE value.

Author(s)

N. Balov

Examples

```
cnet <- cnRandomCatnet(numnodes=20, maxParents=3, numCategories=2)
isDAG(lnodes=cnet@nodes, lpars=cnet@parents)
```

novartis

Novartis multi-tissue data

Description

Consensus Clustering: A re-sampling-based method for class discovery and visualization of gene expression microarray data

Usage

```
data(novartis)
```

Format

A matrix containing 105 observations on 500 genes.

Source

"<http://www.broadinstitute.org/cgi-bin/cancer/datasets.cgi>"

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