

# Package ‘cdcsis’

July 7, 2024

**Type** Package

**Title** Conditional Distance Correlation Based Feature Screening and Conditional Independence Inference

**Description** Conditional distance correlation <[doi:10.1080/01621459.2014.993081](https://doi.org/10.1080/01621459.2014.993081)> is a novel conditional dependence measurement of two multivariate random variables given a confounding variable. This package provides conditional distance correlation, performs the conditional distance correlation sure independence screening procedure for ultrahigh dimensional data <<https://www3.stat.sinica.edu.tw/statistica/J28N1/J28N114/J28N114.html>>, and conducts conditional distance covariance test for conditional independence assumption of two multivariate variable.

**Version** 2.0.4

**Date** 2024-07-09

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**Depends** R(>= 3.0.1)

**Imports** ks (>= 1.8.0), mvtnorm, utils, Rcpp

**Suggests** testthat

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**License** GPL (>= 2)

**NeedsCompilation** yes

**Encoding** UTF-8

**RoxygenNote** 7.1.1

**LinkingTo** Rcpp

**URL** <https://github.com/Mamba413/cdcsis>

**BugReports** <https://github.com/Mamba413/cdcsis/issues>

**Repository** CRAN

**Date/Publication** 2024-07-07 04:40:01 UTC

## Contents

|                          |   |
|--------------------------|---|
| cdcsis-package . . . . . | 2 |
| cdcov . . . . .          | 2 |
| cdcov.test . . . . .     | 4 |
| cdcsis . . . . .         | 6 |

|              |          |
|--------------|----------|
| <b>Index</b> | <b>9</b> |
|--------------|----------|

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| cdcsis-package | <i>Conditional Distance Correlation Based Feature Screening and Conditional Independence Inference</i> |
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### Description

Conditional distance correlation <doi:10.1080/01621459.2014.993081> is a novel conditional dependence measurement of two multivariate random variables given a confounding variable. This package provides conditional distance correlation, performs the conditional distance correlation sure independence screening procedure for ultrahigh dimensional data <doi:10.5705/ss.202014.0117>, and conducts conditional distance covariance test for conditional independence assumption of two multivariate variable.

### Author(s)

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### References

Wang, X., Pan, W., Hu, W., Tian, Y. and Zhang, H., 2015. Conditional distance correlation. Journal of the American Statistical Association, 110(512), pp.1726-1734.

Wen, C., Pan, W., Huang, M. and Wang, X., 2018. Sure independence screening adjusted for confounding covariates with ultrahigh-dimensional data. Statistica Sinica, 28, pp.293-317. URL <http://www3.stat.sinica.edu.tw/statistica/J28N1/28-1.html>

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|-------|---|
| cdcov | <i>Conditional Distance Covariance/Correlation Statistics</i> |
|-------|---|

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### Description

Computes conditional distance covariance and conditional distance correlation statistics, which are multivariate measures of conditional dependence.

### Usage

```
cdcov(x, y, z, width, index = 1, distance = FALSE)
```

```
cdcor(x, y, z, width, index = 1, distance = FALSE)
```

**Arguments**

|          |   |
|----------|---|
| x        | a numeric vector, matrix, or dist object  |
| y        | a numeric vector, matrix, or dist object  |
| z        | z is a numeric vector or matrix. It is the variable being conditioned.  |
| width    | a user-specified positive value (univariate conditional variable) or vector (multivariate conditional variable) for gaussian kernel bandwidth. Its default value is relies on <code>stats::bw.nrd0</code> . |
| index    | exponent on Euclidean distance, in $(0, 2]$   |
| distance | if <code>distance = TRUE</code> , x and y will be considered as distance matrices. Default: <code>distance = FALSE</code> .   |

**Details**

`cdcov` and `cdcor` compute conditional distance covariance and conditional distance correlation statistics. The sample sizes (number of rows or length of the vector) of the two variables must agree, and samples must not contain missing values. If we set `distance = TRUE`, arguments x, y can be a dist object recording distance between samples; otherwise, these arguments are treated as multivariate data.

**Value**

|                    |   |
|--------------------|---|
| <code>cdcov</code> | conditional distance covariance test statistic.     |
| <code>cdcor</code> | conditional distance correlation statistic.         |
| <code>cdc</code>   | conditional distance covariance/correlation vector. |

**Author(s)**

Canhong Wen, Wenliang Pan, and Xueqin Wang

**References**

Wang, X., Pan, W., Hu, W., Tian, Y. and Zhang, H., 2015. Conditional distance correlation. *Journal of the American Statistical Association*, 110(512), pp.1726-1734.

**See Also**

[cdcor](#)

**Examples**

```
library(cdcov)

##### Conditional Distance Covariance #####
set.seed(1)
x <- rnorm(25)
y <- rnorm(25)
z <- rnorm(25)
cdcov(x, y, z)
```

```
##### Conditional Distance Correlation #####
num <- 25
set.seed(1)
x <- rnorm(num)
y <- rnorm(num)
z <- rnorm(num)
cdcov(x, y, z)
```

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cdcov.test

*Conditional Distance Covariance Independence Test*


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### Description

Performs the nonparametric conditional distance covariance test for conditional independence assumption

### Usage

```
cdcov.test(
  x,
  y,
  z,
  num.bootstrap = 99,
  width,
  distance = FALSE,
  index = 1,
  seed = 1,
  num.threads = 1
)
```

### Arguments

|               |  |
|---------------|--|
| x             | a numeric vector, matrix, or dist object   |
| y             | a numeric vector, matrix, or dist object   |
| z             | z is a numeric vector or matrix. It is the variable being conditioned.   |
| num.bootstrap | the number of local bootstrap procedure replications. Default: num.bootstrap = 99.   |
| width         | a user-specified positive value (univariate conditional variable) or vector (multivariate conditional variable) for gaussian kernel bandwidth. Its default value is relies on stats::bw.nrd0 function when conditional variable is univariate, ks::Hpi.diag when conditional variable with at most trivariate, and stats::bw.nrd on the other cases. |
| distance      | if distance = TRUE, x and y will be considered as distance matrices. Default: distance = FALSE.  |
| index         | exponent on Euclidean distance, in (0, 2]  |
| seed          | the random seed  |
| num.threads   | number of threads. Default num.threads = 1.  |

**Value**

cdcov.test returns a list with class "hctest" containing the following components:

|             |  |
|-------------|--|
| statistic   | conditional distance covariance statistic.                     |
| p.value     | the $p$ -value for the test.                                   |
| replicates  | the number of local bootstrap procedure replications.          |
| size        | sample sizes.  |
| alternative | a character string describing the alternative hypothesis.      |
| method      | a character string indicating what type of test was performed. |
| data.name   | description of data.   |

**References**

Wang, X., Pan, W., Hu, W., Tian, Y. and Zhang, H., 2015. Conditional distance correlation. *Journal of the American Statistical Association*, 110(512), pp.1726-1734.

**See Also**

[cdcov](#)

**Examples**

```
library(cdcov)
set.seed(1)
num <- 50
##### Conditional Independent #####
## Case 1:
cov_mat <- matrix(c(1, 0.36, 0.6, 0.36, 1, 0.6, 0.6, 0.6, 1), nrow = 3)
dat <- mvtnorm::rmvnorm(n = num, sigma = cov_mat)
x <- dat[, 1]
y <- dat[, 2]
z <- dat[, 3]
cdcov.test(x, y, z)
## Case 2:
z <- rnorm(num)
x <- 0.5 * (z^3 / 7 + z / 2) + tanh(rnorm(num))
x <- x + x^3 / 3
y <- (z^3 + z) / 3 + rnorm(num)
y <- y + tanh(y / 3)
cdcov.test(x, y, z, num.bootstrap = 99)

##### Conditional Dependent #####
## Case 3:
cov_mat <- matrix(c(1, 0.7, 0.6, 0.7, 1, 0.6, 0.6, 0.6, 1), nrow = 3)
dat <- mvtnorm::rmvnorm(n = num, sigma = cov_mat)
x <- dat[, 1]
y <- dat[, 2]
z <- dat[, 3]
```

```

cdcov.test(x, y, z, width = 0.5)
## Case 4:
z <- matrix(rt(num * 4, df = 2), nrow = num)
x <- z
y <- cbind(sin(z[, 1]) + cos(z[, 2]) + (z[, 3])^2 + (z[, 4])^2,
           (z[, 1])^2 + (z[, 2])^2 + z[, 3] + z[, 4])
z <- z[, 1:2]
cdcov.test(x, y, z, seed = 2)

##### Distance Matrix Input #####
x <- dist(x)
y <- dist(y)
cdcov.test(x, y, z, seed = 2, distance = TRUE)

```

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|        |   |
|--------|---|
| cdcsis | <i>Conditional Distance Correlation Sure Independence Screening (CDC-SIS)</i> |
|--------|---|

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### Description

Performs conditional distance correlation sure independence screening (CDC-SIS).

### Usage

```

cdcsis(
  x,
  y,
  z = NULL,
  width,
  threshold = nrow(y),
  distance = FALSE,
  index = 1,
  num.threads = 1
)

```

### Arguments

|                    |   |
|--------------------|---|
| <code>x</code>     | a numeric matrix, or a list which contains multiple numeric matrix  |
| <code>y</code>     | a numeric vector, matrix, or dist object  |
| <code>z</code>     | <code>z</code> is a numeric vector or matrix. It is the variable being conditioned.   |
| <code>width</code> | a user-specified positive value (univariate conditional variable) or vector (multivariate conditional variable) for gaussian kernel bandwidth. Its default value is relies on <code>stats::bw.nrd0</code> function when conditional variable is univariate, <code>ks::Hpi.diag</code> when conditional variable with at most trivariate, and <code>stats::bw.nrd</code> on the other cases. |

|             |   |
|-------------|---|
| threshold   | the threshold of the number of predictors recruited by CDC-SIS. Should be less than or equal than the number of column of $x$ . Default value threshold is sample size. |
| distance    | if distance = TRUE, only $y$ will be considered as distance matrices. Default: distance = FALSE   |
| index       | exponent on Euclidean distance, in $(0, 2]$   |
| num.threads | number of threads. Default num.threads = 1.   |

**Value**

|       |   |
|-------|---|
| ix    | the vector of indices selected by CDC-SIS   |
| cdcor | the conditional distance correlation for each univariate/multivariate variable in $x$ |

**Author(s)**

Canhong Wen, Wenliang Pan, Mian Huang, and Xueqin Wang

**References**

Wen, C., Pan, W., Huang, M. and Wang, X., 2018. Sure independence screening adjusted for confounding covariates with ultrahigh-dimensional data. *Statistica Sinica*, 28, pp.293-317. URL <http://www3.stat.sinica.edu.tw/statistica/J28N1/J28N114/J28N114.html>

**See Also**

[cdcor](#)

**Examples**

```
## Not run:

library(cdcsis)

##### univariate explanative variables #####
set.seed(1)
num <- 100
p <- 150
x <- matrix(rnorm(num * p), nrow = num)
z <- rnorm(num)
y <- 3 * x[, 1] + 1.5 * x[, 2] + 4 * z * x[, 5] + rnorm(num)
res <- cdcsis(x, y, z)
head(res[["ix"]], n = 10)

##### multivariate explanative variables #####
x <- as.list(as.data.frame(x))
x <- lapply(x, as.matrix)
x[[1]] <- cbind(x[[1]], x[[2]])
x[[2]] <- NULL
res <- cdcsis(x, y, z)
```

```
head(res[["ix"]], n = 10)

##### multivariate response variables #####
num <- 100
p <- 150
x <- matrix(rnorm(num * p), nrow = num)
z <- rnorm(num)
y1 <- 3 * x[, 1] + 5 * z * x[, 4] + rnorm(num)
y2 <- 3 * x[, 2] + 5 * x[, 3] + 2 * z + rnorm(num)
y <- cbind(y1, y2)
res <- cdcsis(x, y, z)
head(res[["ix"]], n = 10)

## End(Not run)
```



# Index

cdcor, [3](#), [7](#)  
cdcor (cdcov), [2](#)  
cdcov, [2](#), [5](#)  
cdcov.test, [4](#)  
cdcsis, [6](#)  
cdcsis-package, [2](#)