

Package ‘simdd’

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Type Package

Title Simulation of Fisher Bingham and Related Directional Distributions

Version 1.1-1

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Description Simulation methods for the Fisher Bingham distribution on the unit sphere, the matrix Bingham distribution on a Grassmann manifold, the matrix Fisher distribution on $SO(3)$, and the bivariate von Mises sine model on the torus.

The methods use the first ever general purpose acceptance/rejection simulation algorithm for the Bingham distribution and are described fully by Kent, Ganeiber and Mardia (2018) <[doi:10.1080/10618600.2017.1390468](https://doi.org/10.1080/10618600.2017.1390468)>.

These methods superseded earlier MCMC simulation methods and are more general than earlier simulation methods.

The methods can be slower in specific situations where there are existing non-MCMC simulation methods (see Section 8 of Kent, Ganeiber and Mardia (2018) <[doi:10.1080/10618600.2017.1390468](https://doi.org/10.1080/10618600.2017.1390468)> for further details).

License GPL-2

Suggests CircStats

NeedsCompilation no

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R topics documented:

simdd-package	2
Simulate Fisher Bingham and related distributions	3

Index	6
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simdd-package

simdd – Simulation of Fisher Bingham and Related Directional Distributions

Description

Simulation methods for the Fisher Bingham distribution on the unit sphere, the matrix Bingham distribution on a Grassmann manifold, the matrix Fisher distribution on $SO(3)$, and the bivariate von Mises sine model on the torus. The methods use the first ever general purpose acceptance/rejection simulation algorithm for the Bingham distribution and are described fully by Kent, Ganeiber and Mardia (2018). These methods superseded earlier MCMC simulation methods and are more general than earlier simulation methods. The methods can be slower in specific situations where there are existing non-MCMC simulation methods (see Section 8 of Kent, Ganeiber and Mardia (2018) for further details).

Details

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Author(s)

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References

John T. Kent, Asaad M. Ganeiber & Kanti V. Mardia (2018) A New Unified Approach for the Simulation of a Wide Class of Directional Distributions, *Journal of Computational and Graphical Statistics*, 27:2, 291-301, DOI: [doi:10.1080/10618600.2017.1390468](https://doi.org/10.1080/10618600.2017.1390468)

Examples

```
# simulate 20 random unit vectors from a Bingham distribution
# with concentration matrix diag(c(1,2,-3)).
X=rBingham(20,c(1,2,-3))
# check the efficiency of the simulation algorithm
attr(X,"summary")
```

 Simulate Fisher Bingham and related distributions

Simulate Fisher Bingham and related distributions

Description

Simulate the Fisher Bingham distribution on the unit sphere, the matrix Bingham distribution on a Grassmann manifold, the matrix Fisher distribution on SO(3), and the bivariate von Mises sin model on the torus = product of two circles.

Usage

```
rFisherBingham(nsim, mu = 0, Aplus = 0, q = dimset(mu, Aplus), mtop = 1000)
rBingham(nsim, Aplus, q = dimq(Aplus), mtop = 1000)
rBingham.Grassmann(nsim, Aplus = 0, q = dimq(Aplus), r = 1, mtop = 1000)
rFisher.S03(nsim, Fmat)
rvMsin.torus(nsim, k1, k2, alpha, mtop=1000)
rBessel(nsim, k1, k2, alpha, mtop=1000)
```

Arguments

nsim	the desired number of simulations
mu	a vector of length q. If mu is entered as a scalar, it is interpreted as the vector (0, ..., 0, mu) with zeros except in the final coordinate.
Aplus	a symmetric q by q matrix. If Aplus is given as a scalar, it is interpreted as the q by q matrix of zeros. If Aplus is given as a vector, it is interpreted as the matrix diag(Aplus).
q	The simulation is done on the unit sphere in R^q . Thus for the circle, q=2. Note that q only needs to be given explicitly if both mu and Aplus are scalars. In the default setting the internal function dimset, q=dimset(mu, Aplus), determines q from the length of mu or the dimension of Aplus, if it can.
r	For rBingham.Grassmann, r denotes the number of columns ($1 \leq r \leq q-1$) in the matrix Bingham distribution
mtop	An internal parameter, designed to prevent infinite loops.
Fmat	The 3 by 3 parameter matrix for the matrix Fisher distribution in the function rFisher.S03.
k1, k2, alpha	The two concentration parameters and the interaction parameter in the function rvMsin.torus.

Details

The Fisher Bingham distribution on the unit sphere in R^q has density proportional to

$$\exp(\mu^T x + x^T \text{Aplus} x)$$

where x is a unit vector in R^q , and μ (q -dimensional vector) and A plus (q by q symmetric) are parameters.

The matrix Bingham distribution on q by r matrices X whose columns are orthonormal, is given by the density proportional to

$$\exp(\text{trace}(X^T A \text{plus} X)).$$

The Bingham distribution on the unit sphere in R^q can be simulated using (a) `rBingham`, (b) `rFisherBingham` with $\mu=0$, and (c) `rBingham.Grassmann` with $r=1$. Choice (a) will be fastest.

The Fisher distribution can be simulated using `rFisherBingham` with A plus $=0$.

The matrix Fisher distribution on $SO(3)$ has density proportional to

$$\exp(\text{trace}(F \text{mat}^T X))$$

where X is a 3 by 3 rotation matrix, and $F \text{mat}$ is a 3 by 3 parameter matrix.

The bivariate von Mises sine model on the torus has density proportional to

$$\exp(k_1 \cos(\theta) + k_2 \cos(\phi) + \alpha \sin(\theta) \sin(\phi))$$

for two angles θ, ϕ . The Bessel density is obtained from the bivariate von Mises sine model as the marginal density of θ .

Value

For `rBingham` and `rFisherBingham`, the output is an `nsim` by `q` matrix. Each row is a simulated unit vector.

For `rBingham.Grassmann`, the output is an `nsim` by `q` by `r` array. For each value of the first index, the result is a simulated `q` by `r` matrix with orthonormal columns.

For `rFisher.S03`, the output is an `nsim` by `r` by `r` array. For each value of the first index, the result is a simulated `r` by `r` matrix rotation matrix.

For `rvMsin.torus`, the output is an `nsim` by 4 matrix, with each row containing the simulated value of $(\cos(\theta), \sin(\theta), \cos(\phi), \sin(\phi))$.

For `rBessel`, the output is an `nsim` by 2 matrix containing the marginal simulated values of $(\cos(\theta), \sin(\theta))$.

In all cases, the output has an attribute `summary`, which is a vector of length 6 summarizing some details about the number of simulations needed in the acceptance/rejection algorithm. The key element of this vector is called `efficiency`, a number between 0 and 1, where 1 means that all the simulated values from the envelope distribution have been accepted.

Author(s)

J T Kent

References

John T. Kent, Asaad M. Ganeiber & Kanti V. Mardia (2018) A New Unified Approach for the Simulation of a Wide Class of Directional Distributions, *Journal of Computational and Graphical Statistics*, 27:2, 291-301, DOI: [doi:10.1080/10618600.2017.1390468](https://doi.org/10.1080/10618600.2017.1390468)

See Also

The function `rvm` in the CRAN library `CircStats` provides a more efficient method to simulate from the von Mises distribution (i.e. the Fisher distribution with $q=2$) than `rFisherBingham`.

Examples

```
X1=rBingham(10,c(1,2,-3))
attr(X1,"summary")
X2=rFisherBingham(10,c(3,2,1),c(1,2,-3))
X3=rBingham.Grassmann(10,c(1,2,-3),r=2)
X4=rFisher.S03(10,matrix(c(1,2,3,4,2,1,0,1,2),3,3))
X5=rvMsin.torus(10,2.2,3.1,1.3)
X6=rBessel(10,2.2,3.1,1.3)
```

Index

rBessel (Simulate Fisher Bingham and related distributions), [3](#)
rBingham (Simulate Fisher Bingham and related distributions), [3](#)
rFisher.S03 (Simulate Fisher Bingham and related distributions), [3](#)
rFisherBingham (Simulate Fisher Bingham and related distributions), [3](#)
rvm, [5](#)
rvMsin.torus (Simulate Fisher Bingham and related distributions), [3](#)

simdd (simdd-package), [2](#)
simdd-package, [2](#)
Simulate Fisher Bingham and related distributions, [3](#)